

**Ground motion measurement in the Lake
Mead area, Nevada, by differential SAR
interferometry time series analysis: Probing
the lithosphere rheological structure**

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How does the crust and uppermost mantle respond to stress at short time scale ?

Elastic response

At least for time scales up to 1 year

Visco-elastic response

* Post-glacial rebound : ~3000 years.

Mean mantle viscosity 10^{21} Pa.s

$$\tau \sim \eta \dot{\epsilon} / \rho g$$

Depth + lateral variations of viscosity

* Isostatic rebound of palaeo-lakes

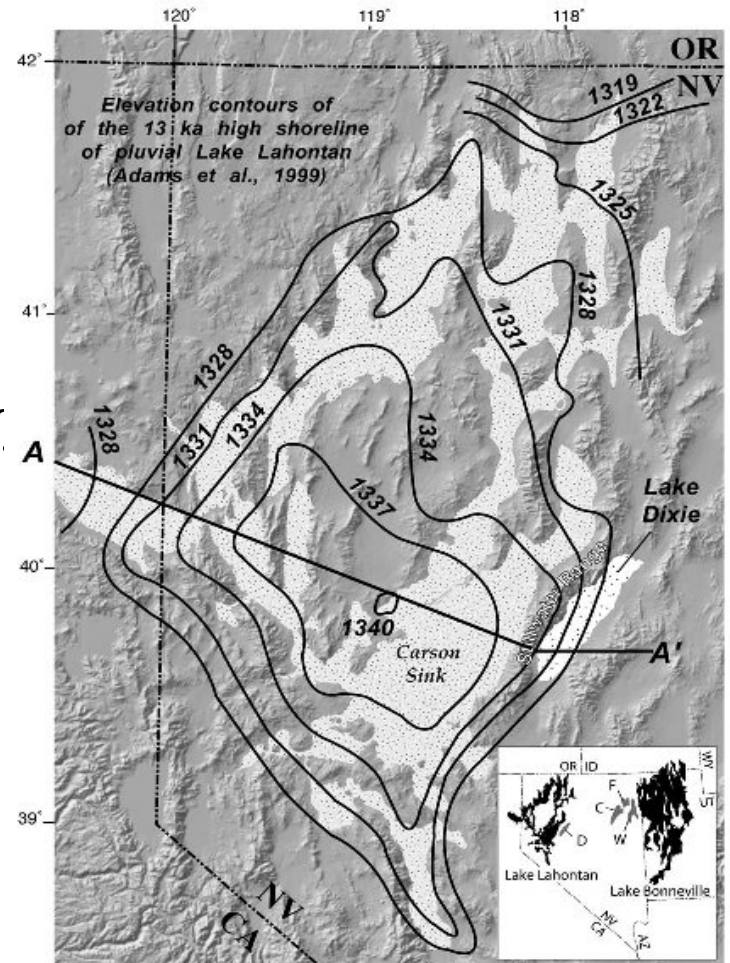
Lake Bonneville, Lake Lahontan

300 years,

viscosity of 4×10^{17} to 10^{19} Pa.s

* Post-seismic rebound:

transient rheologies with low viscosity

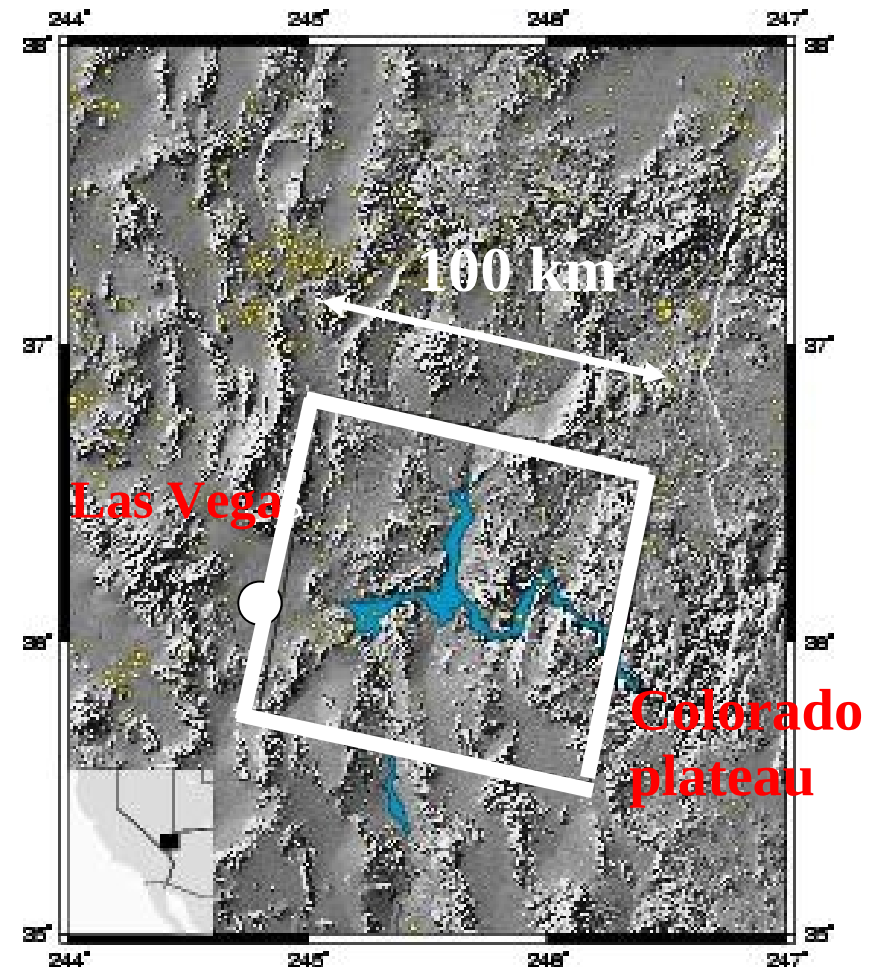
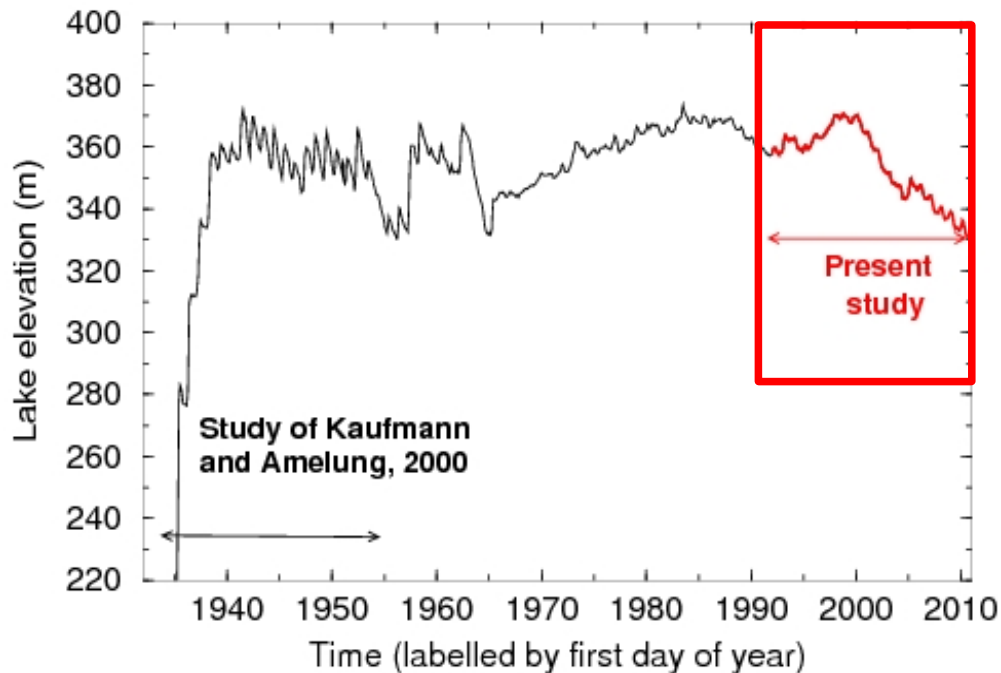


Shorelines elevation, Lake Lahontan
Adams et al., 1999

Surface load : Lake Mead water level fluctuations

In the Basin and Range,
Nevada, Arizona, USA :

- thin lithosphere
- desert



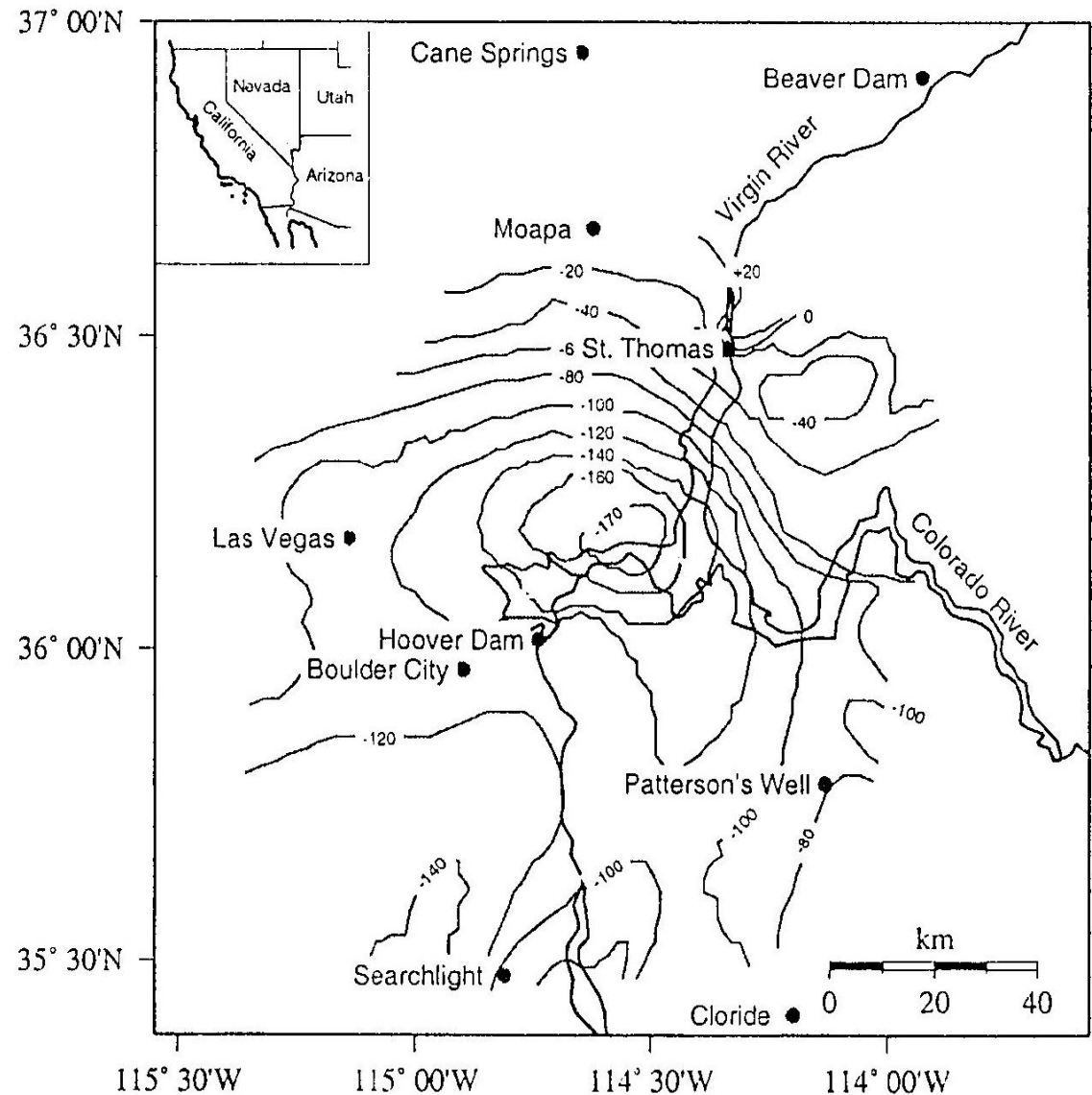
Study of Kaufmann and Amelung (2000) : 1935-1965

- Impoundment in 1935 was followed by a delayed subsidence : 17 cm between 1935 and 1950
(Longwell, 1960)

- Elastic thickness : 32 km

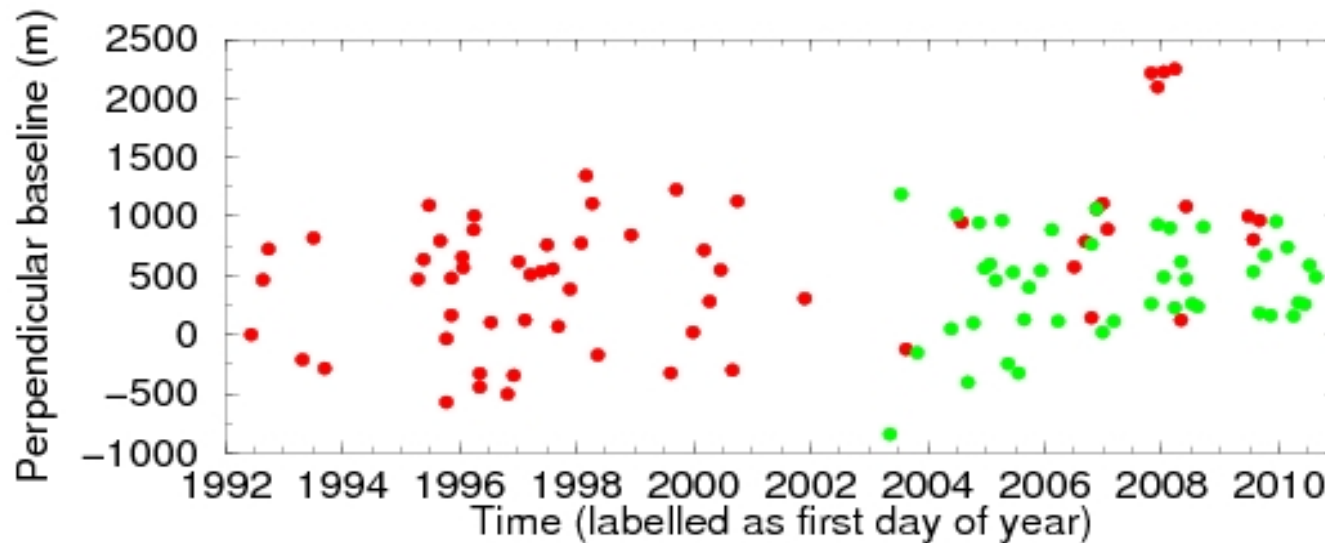
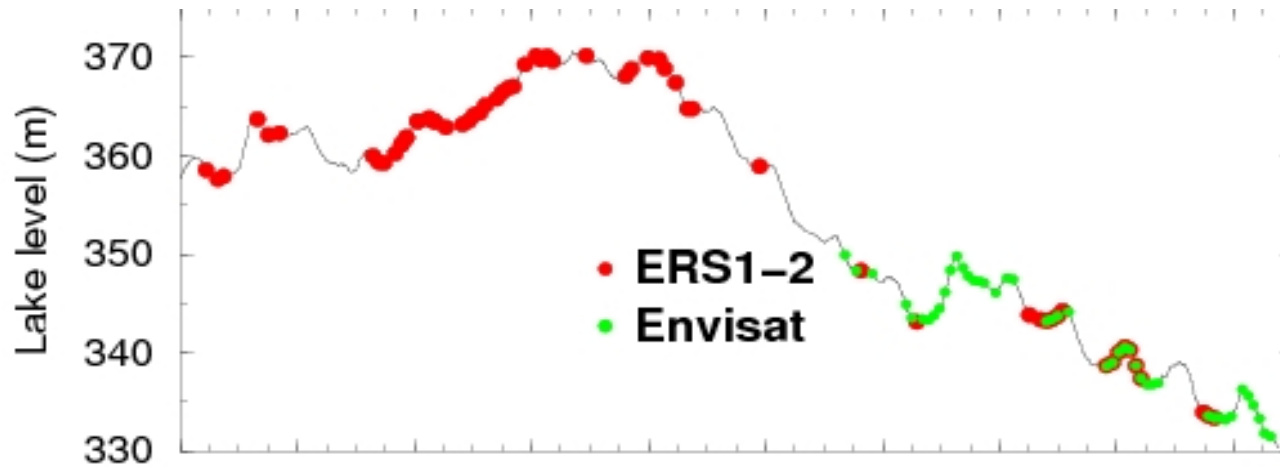
Mantle viscosity : 10^{18} Pa s

Relaxation time : 25 yrs



Subsidence map derived from leveling surveys results

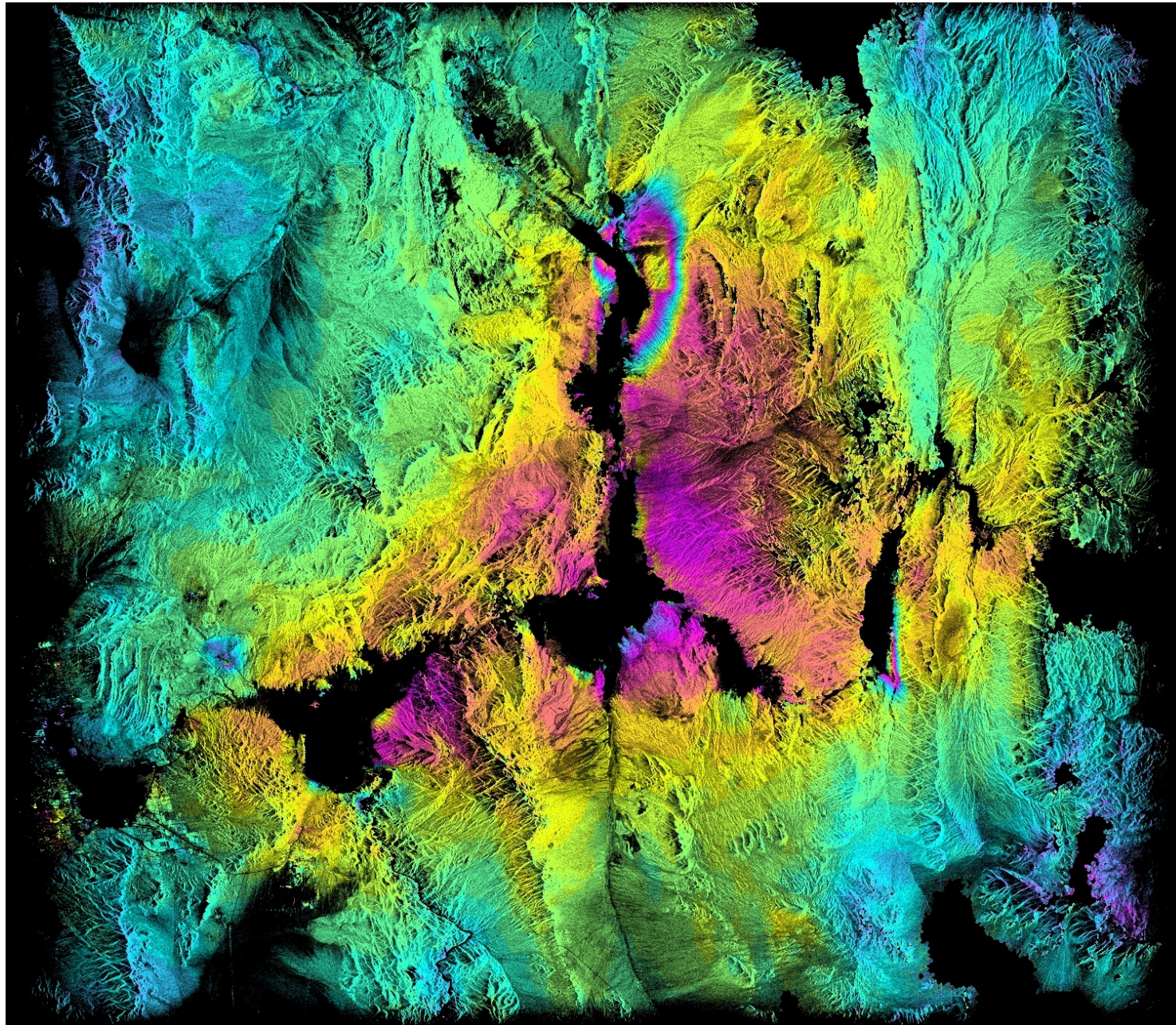
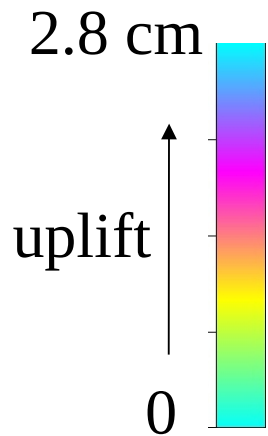
SAR data : 63 ERS acquisitions, 45 Envisat acquisitions
analysed with a Small BASeline approach (Schmidt and Bürgmann, 2003)



553 interferograms :
very high network
redundancy

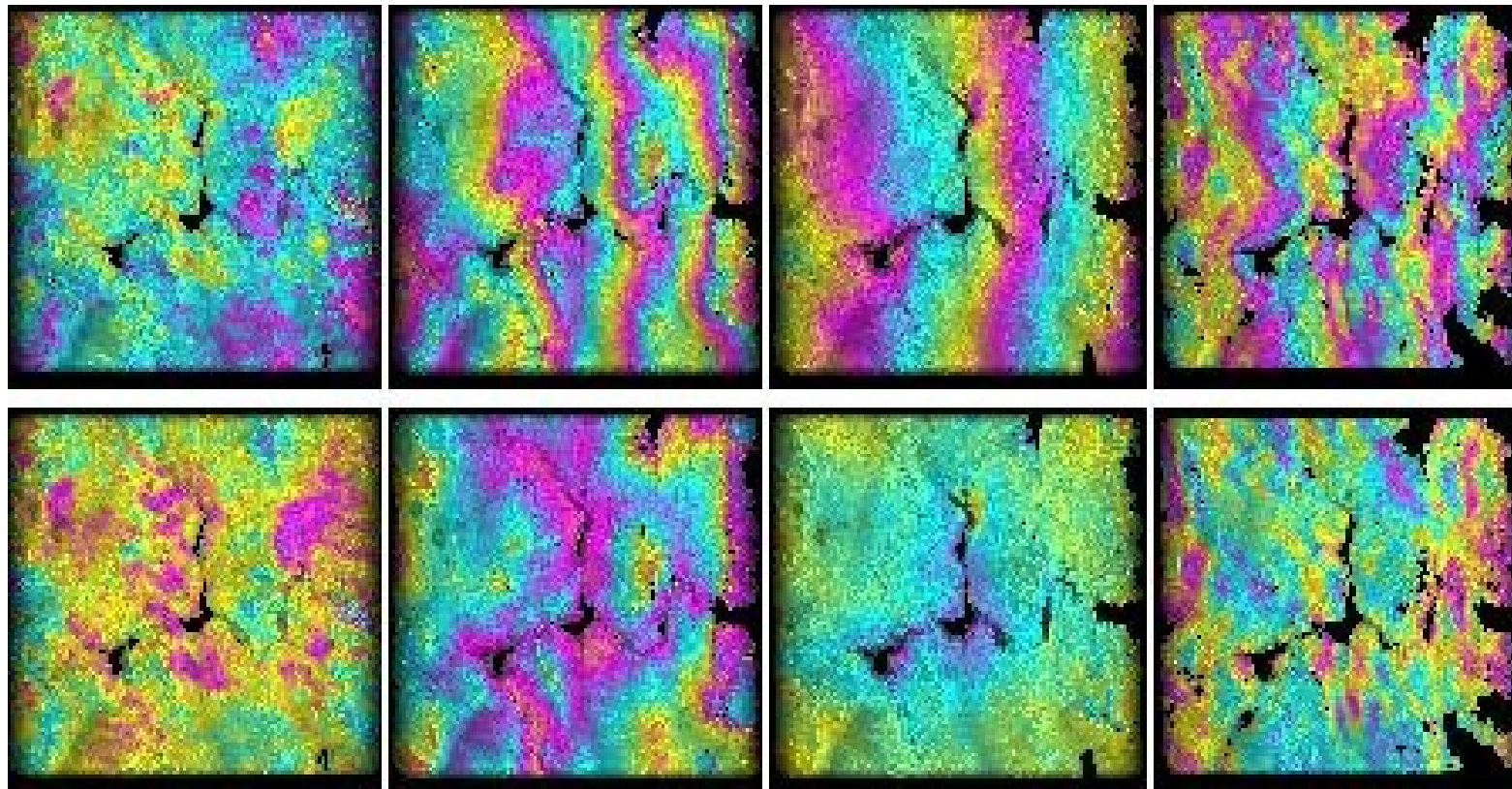
ERS (pre-2001)-ERS(post 2002) interferograms :

1996-03-30 to 2006-11-19 : water decline by 20 m, up to 2.5 cm of uplift



553 Differential SBAS interferograms

= Orbit error (~ 5 cm) + Atmospheric delays (~ 4 cm)
+ ground motion (~ 2 cm) + noise



Remove
“twisted”
plane

(a) 1995/04/05-
1997/03/16

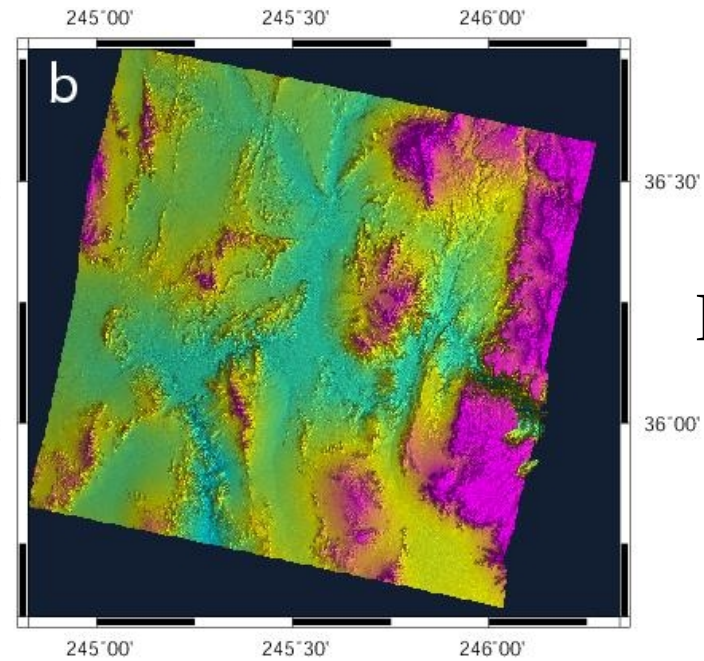
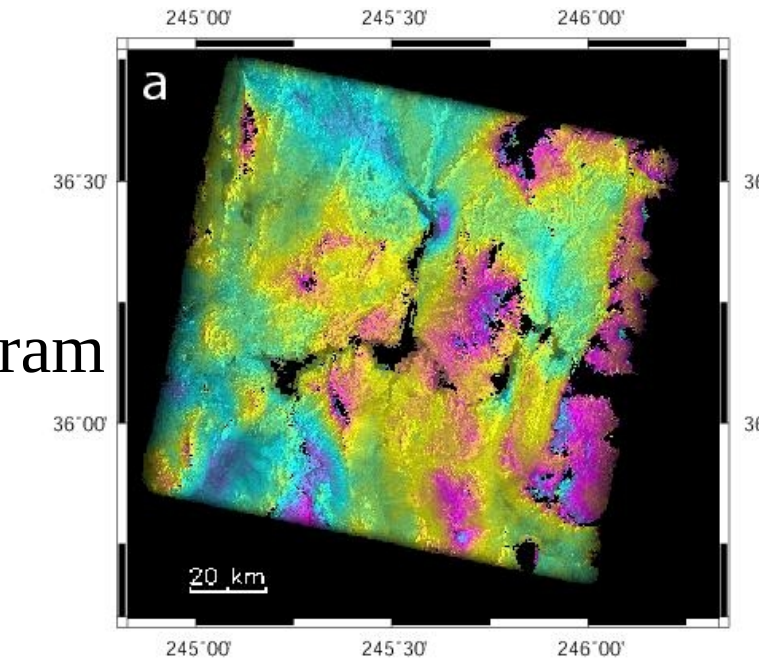
(b) 1995/11/12-
1997/01/15

(c) 1996/01/20-
1998/01/25

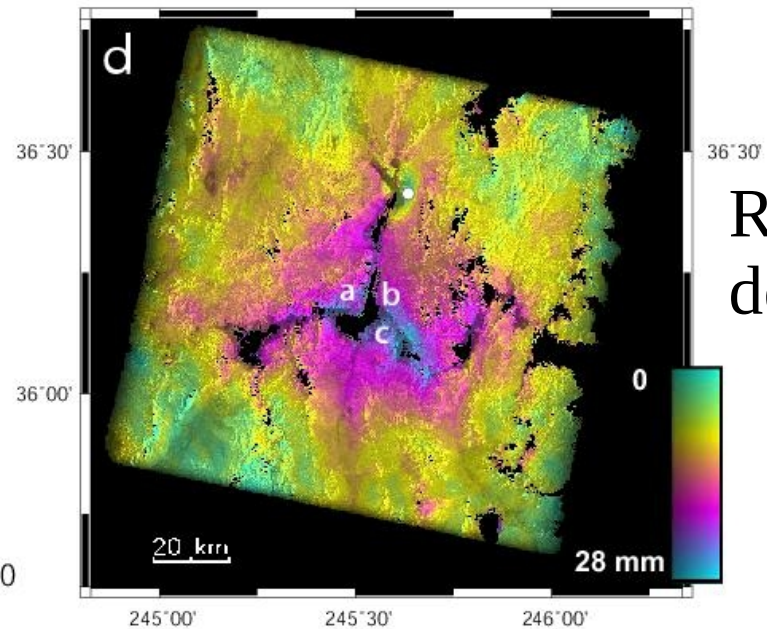
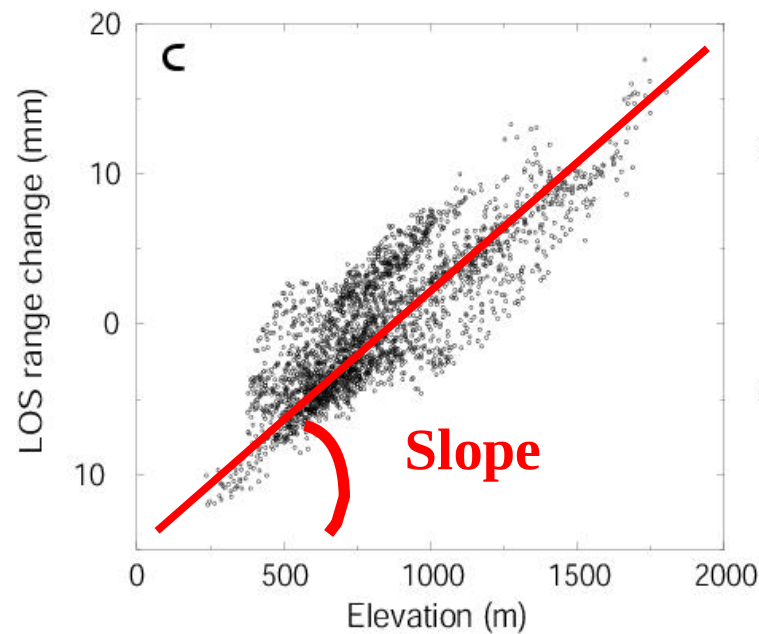
(d) 1997/02/09-
2001/11/25

Atmospheric delays : Phase-elevation correlation

Interferogram

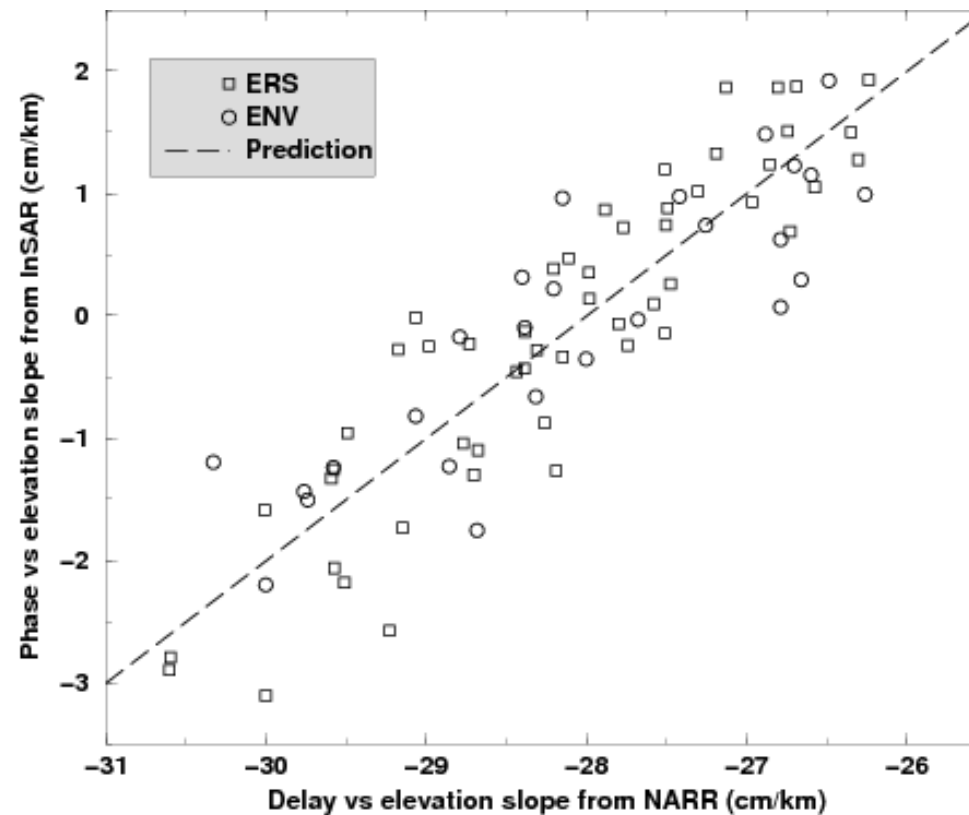


DEM



Residue :
deformation

Phase-elevation correlation : comparison with predictions derived from the North American Regional Analysis

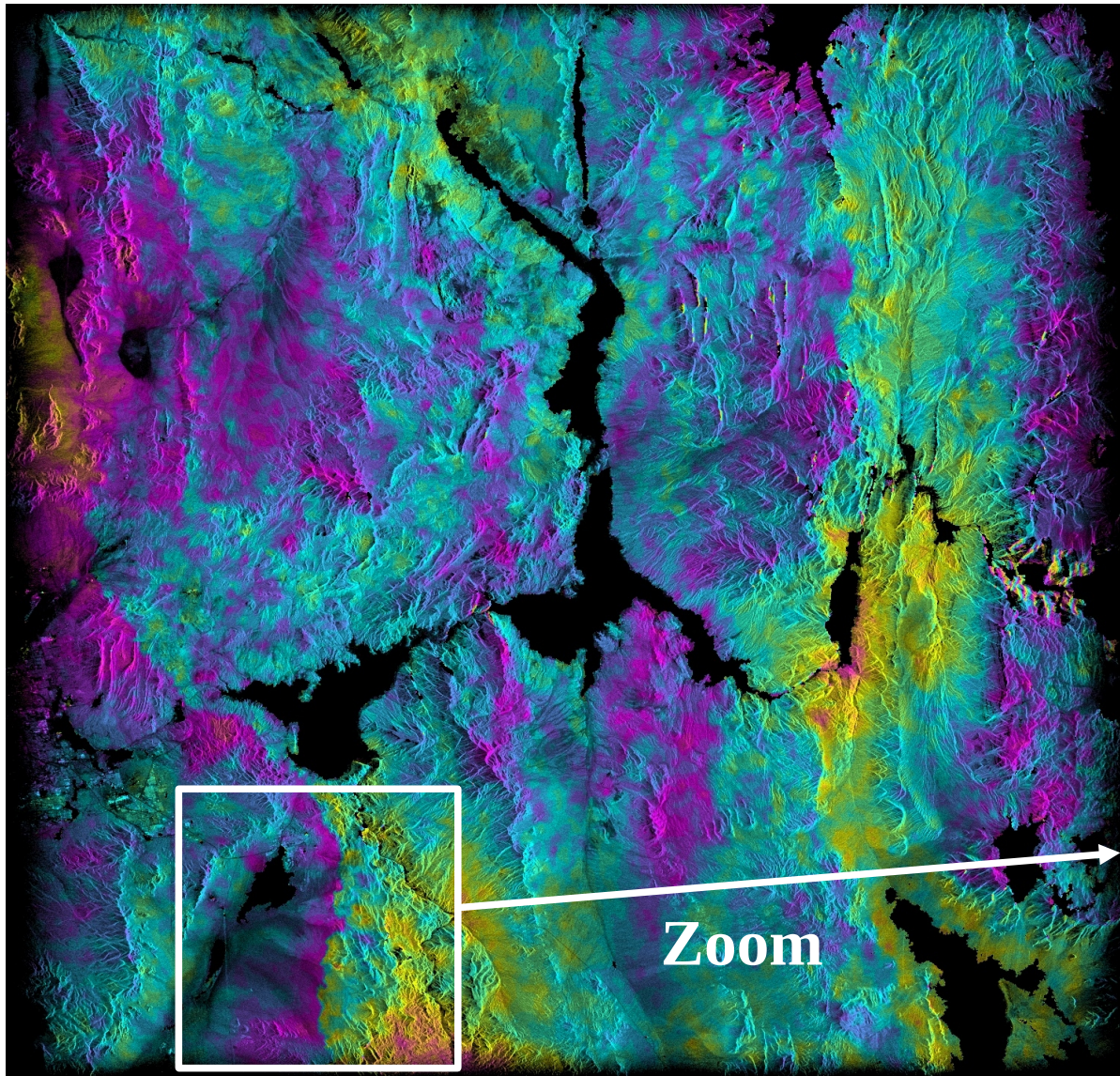


COMPARISON
DInSAR
versus
NARR prediction

Doin et al.,
J. of Applied
Geophys., 2009

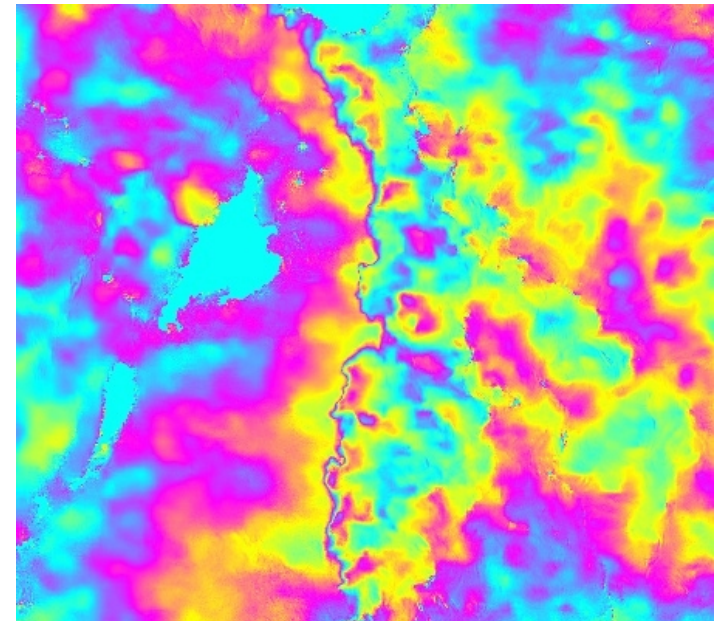
Random patterns

Ripples, bubbles, patches, fronts,



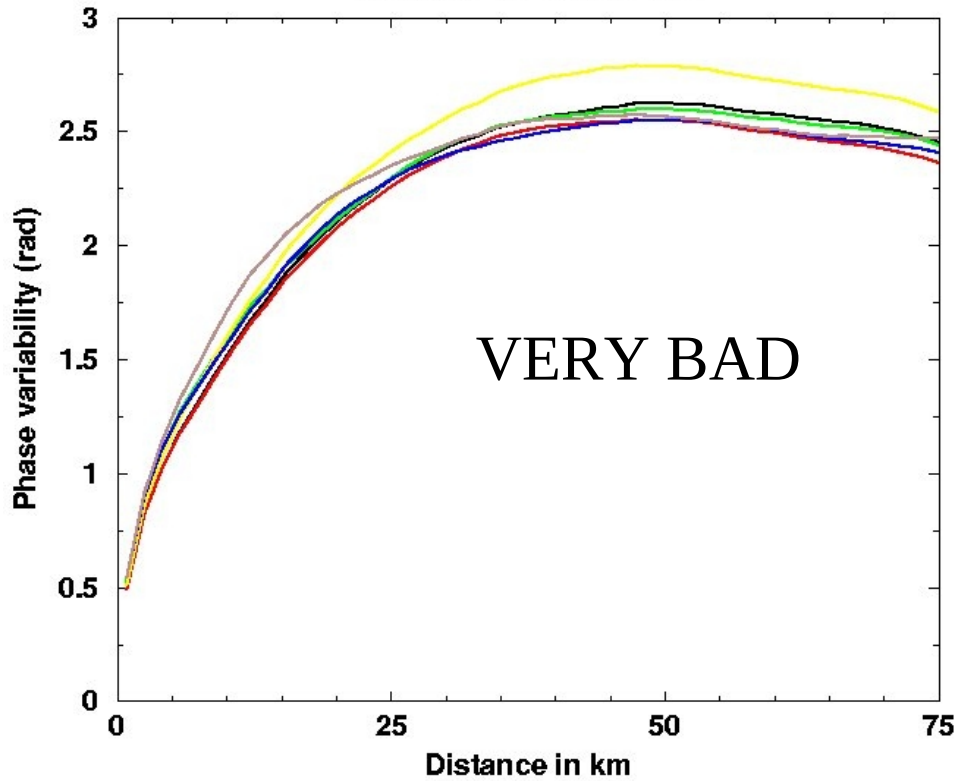
1992-08-20 1995-04-15
1 color cycle = 5.6 cm

1 color cycle = 2.8 cm

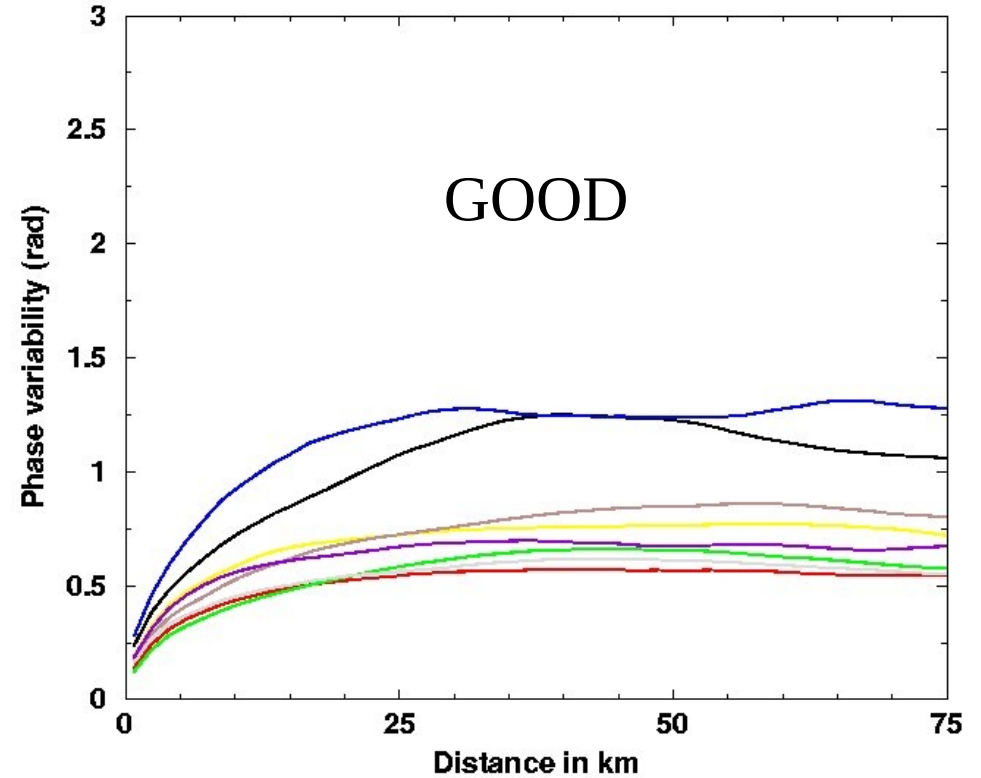


Random patterns : compute structure functions for each interferogram

June : 18-06-2000 (ERS)



February : 27-02-2005 (ENVISAT)



==> After network inversion:
Amplitude of turbulent atmosphere (APS) for each date

Inversion of interferograms into time series

- Use 553 corrected interferograms based on 107 acquisitions, invert for successive increments of phase delays
- Check for unwrapping errors using the strong interferometric network redundancy and correction
- Link the ERS and Envisat time series by adjusting the phase of acquisitions 30 min apart
- Invert the DEM error and correct the phase of each acquisition accordingly

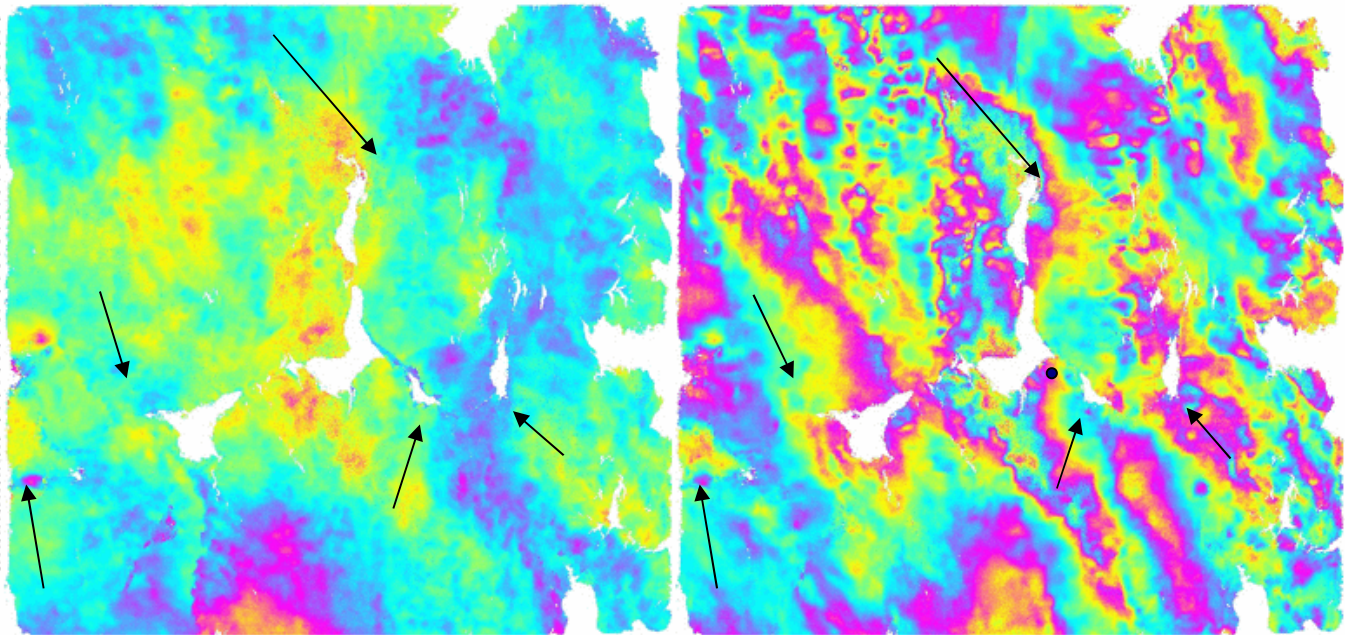
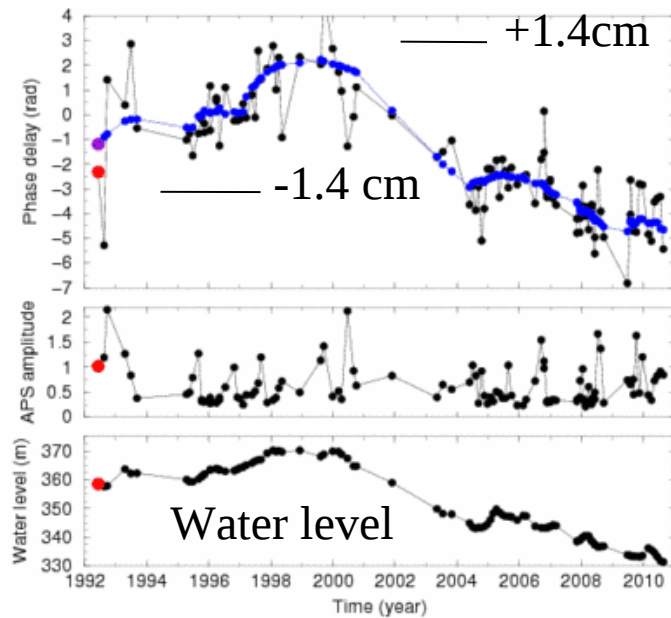
==> Time series of raw phase delay maps at each acquisition date (including mainly deformation and turbulent atmosphere)

==> Smoothed time series which contains mostly deformation

Separation of signals : atmosphere / hydrology / effect of water load

Smoothed time series :
mainly deformation

Raw phase delay:
turbulent atmospheric patterns
+ deformation

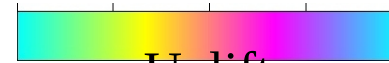


DEF_19920611.jpg

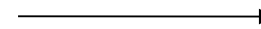
TOT_19920611.jpg

0

1.8 cm



Uplift



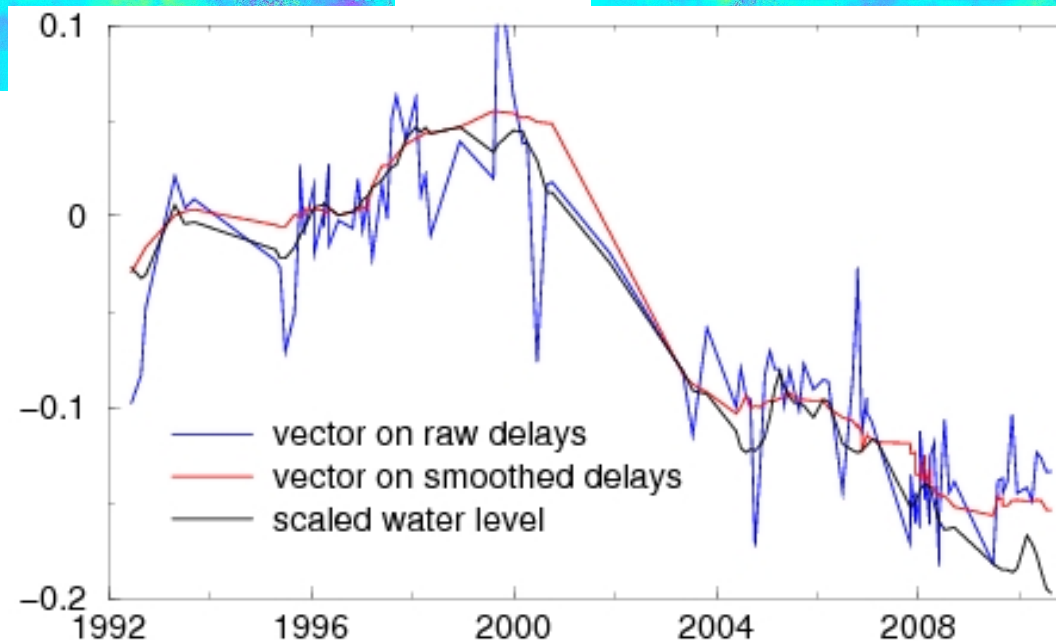
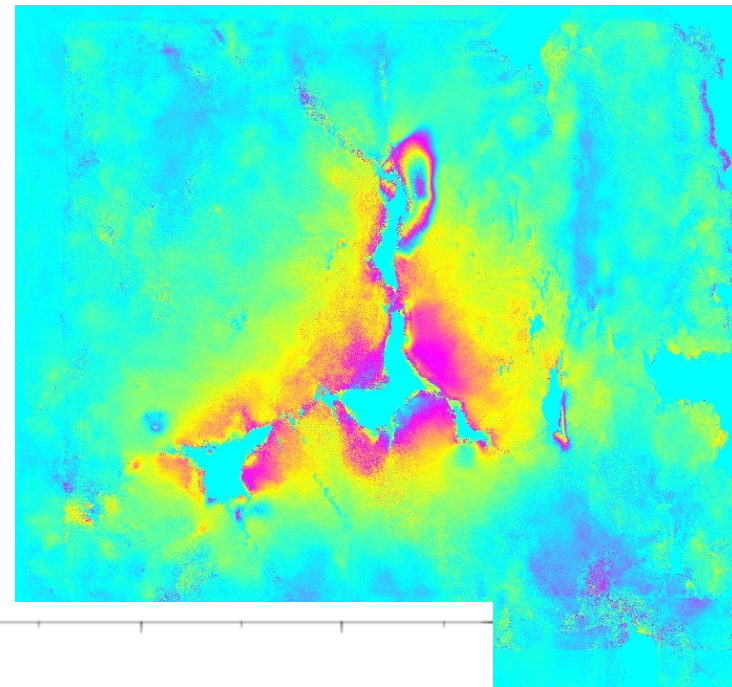
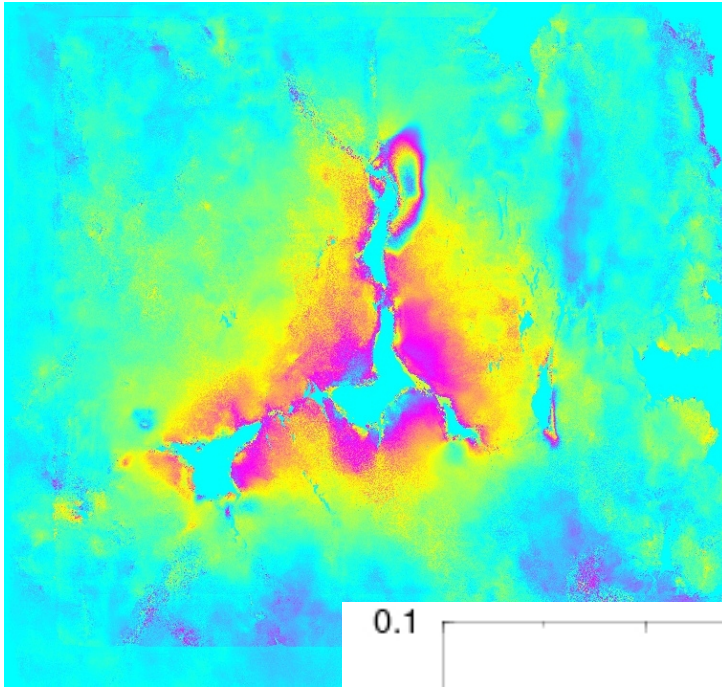
Smoothing weighted by the amplitude of atmospheric patterns

Separation of signals : Principal Component Analysis

First eigen vector:

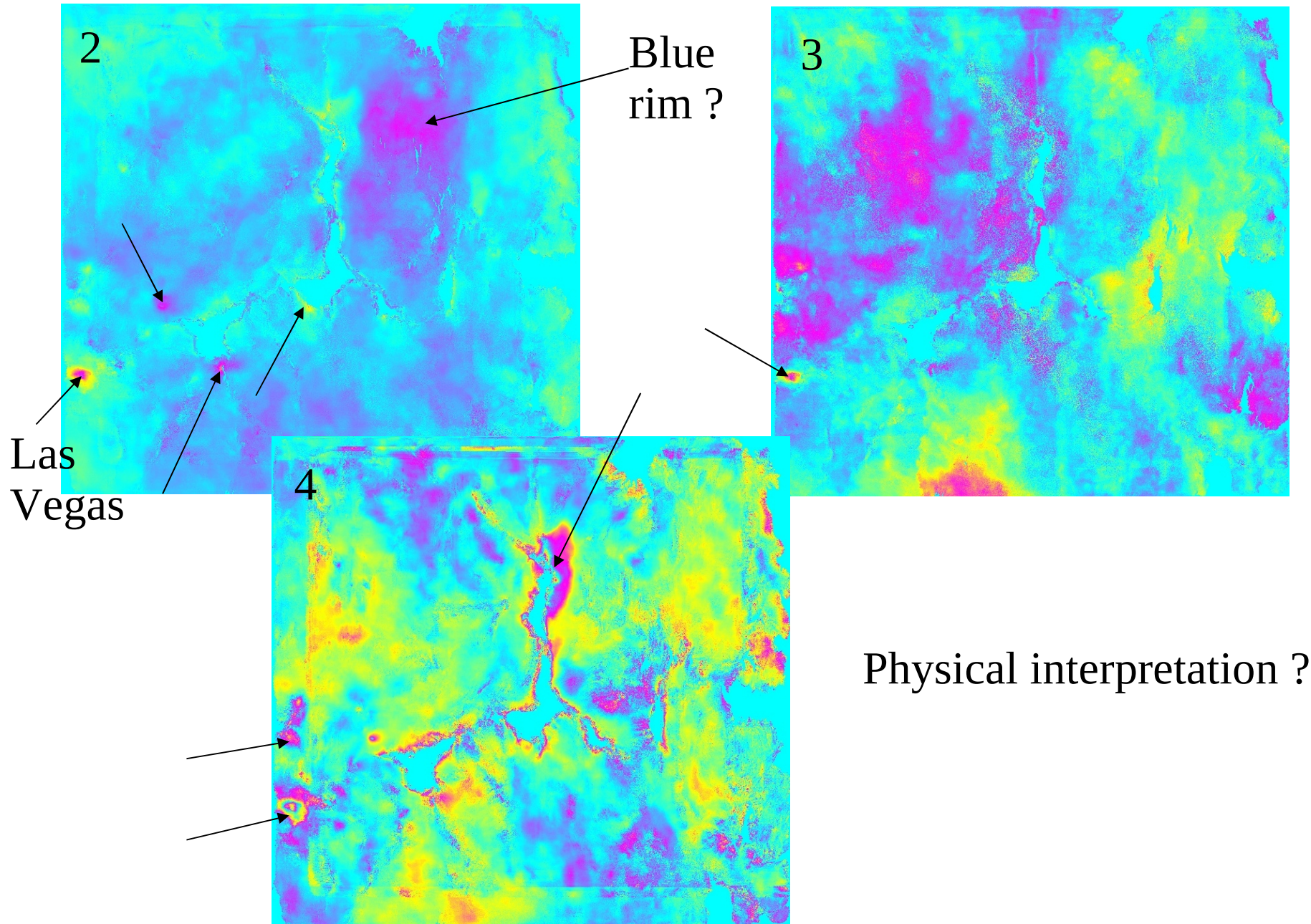
On raw phase delays

On smoothed phase delays



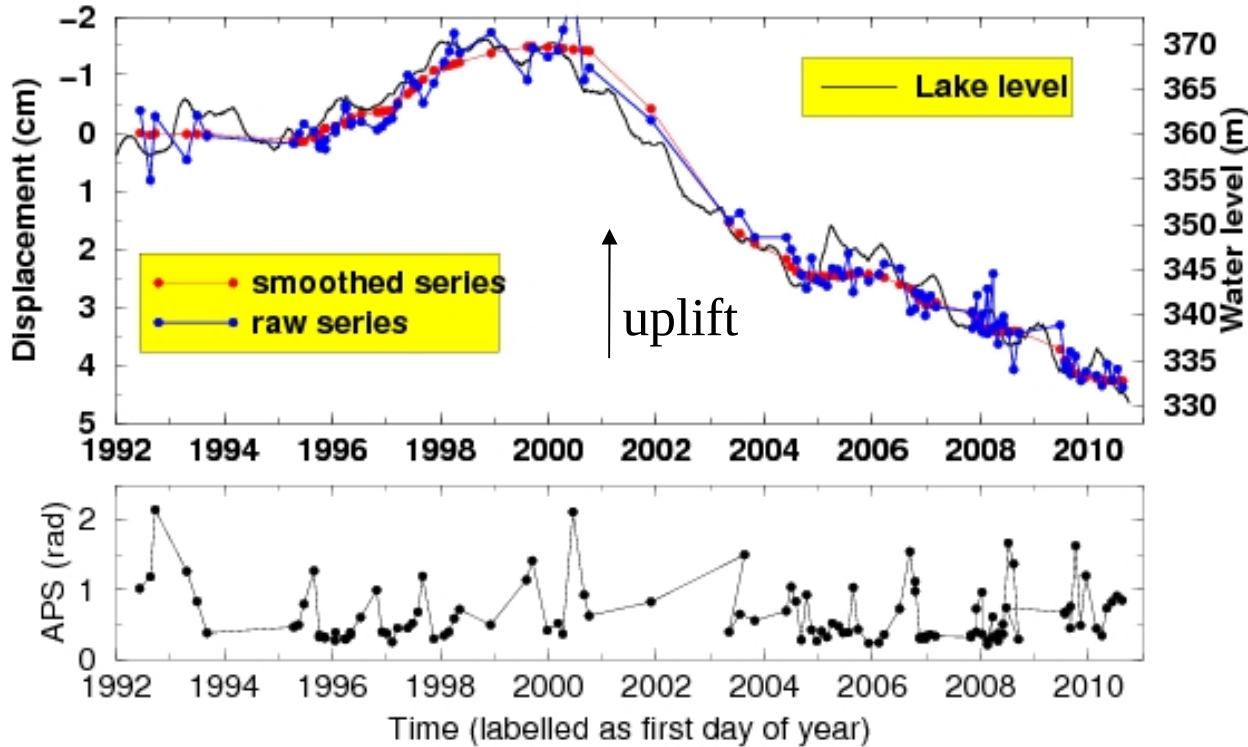
Separation of signals : Principal Component Analysis

Following eigen vectors on smoothed phase delays

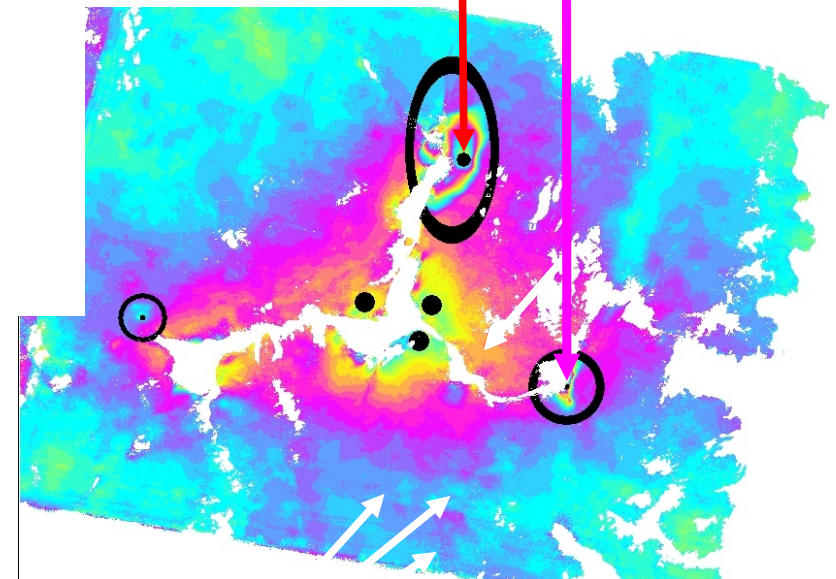


Physical interpretation ?

Hydrological signals :

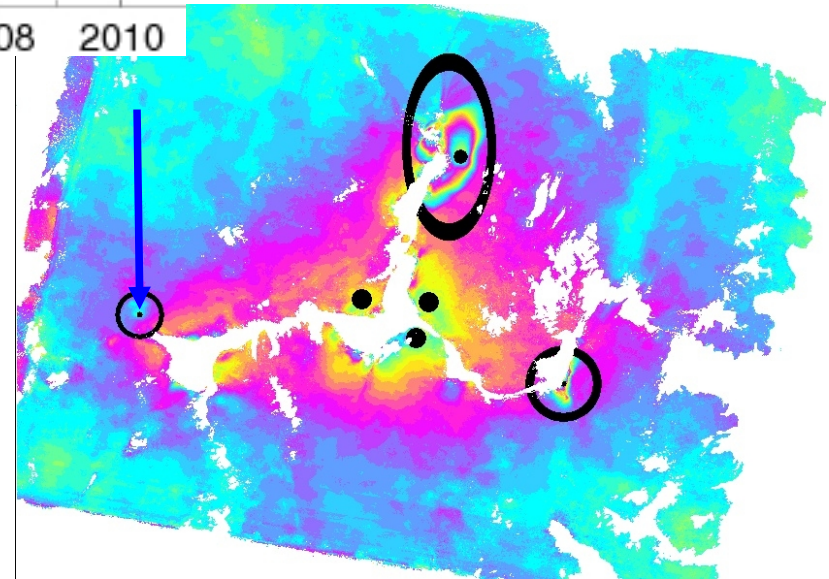
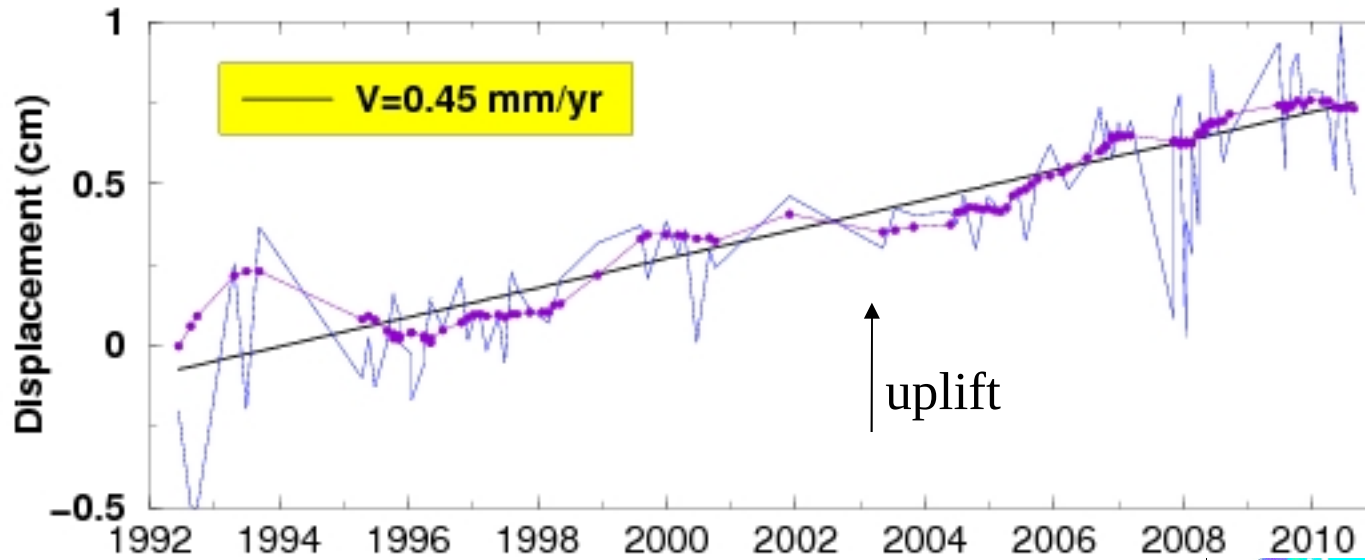


~3months delay between ground motion and lake level change : water diffusion



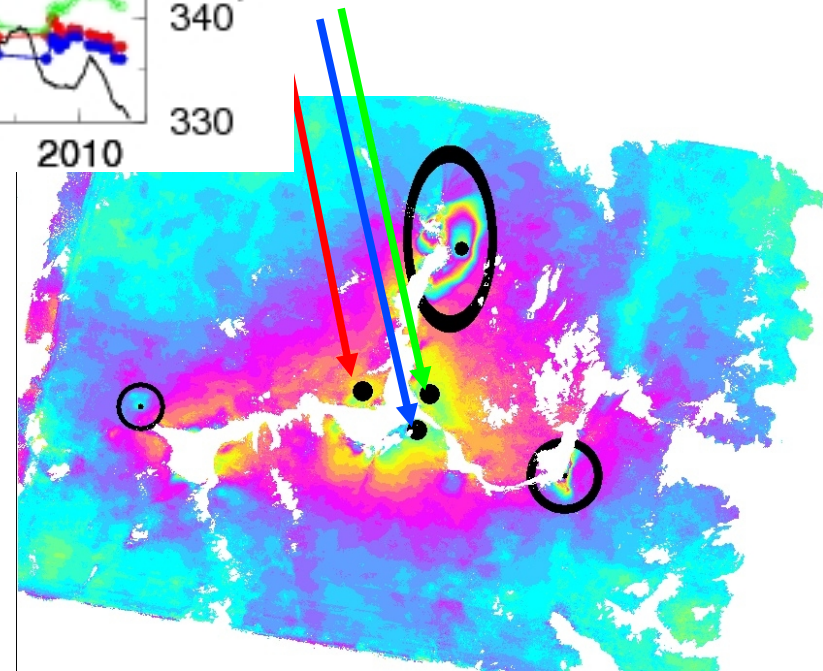
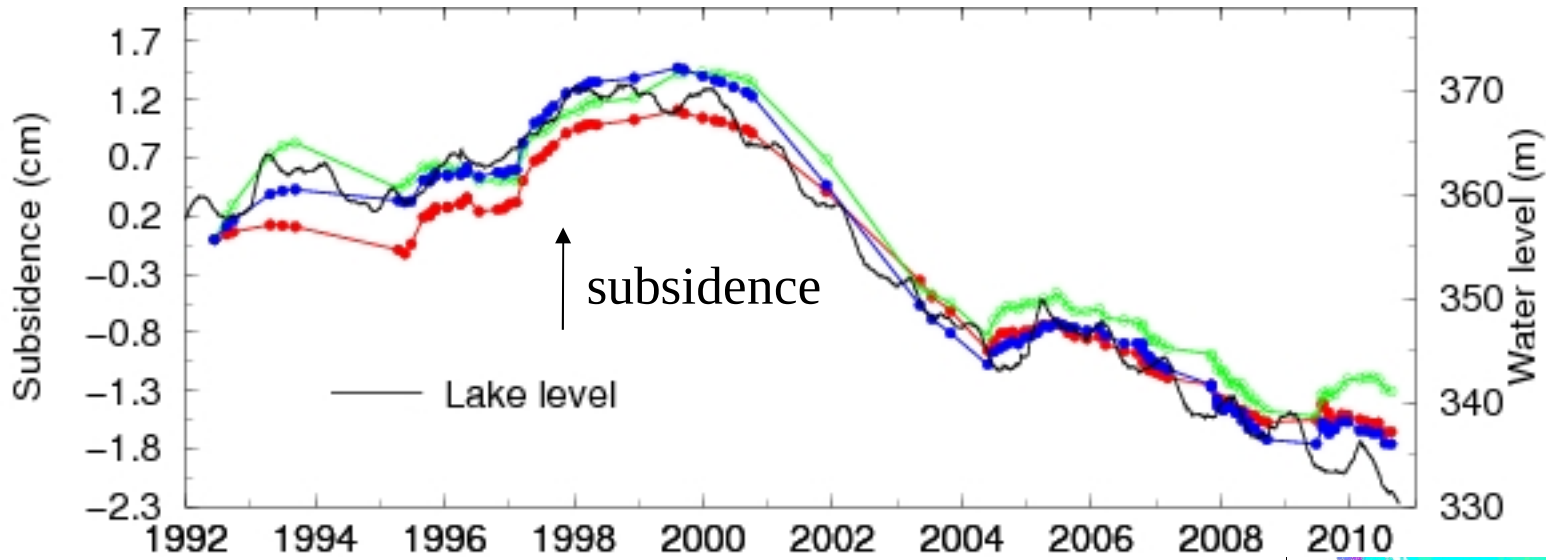
Regression coefficient between data and lake level

Hydrologic signals



Regression coefficient between data and lake level

Effect of water load fluctuations



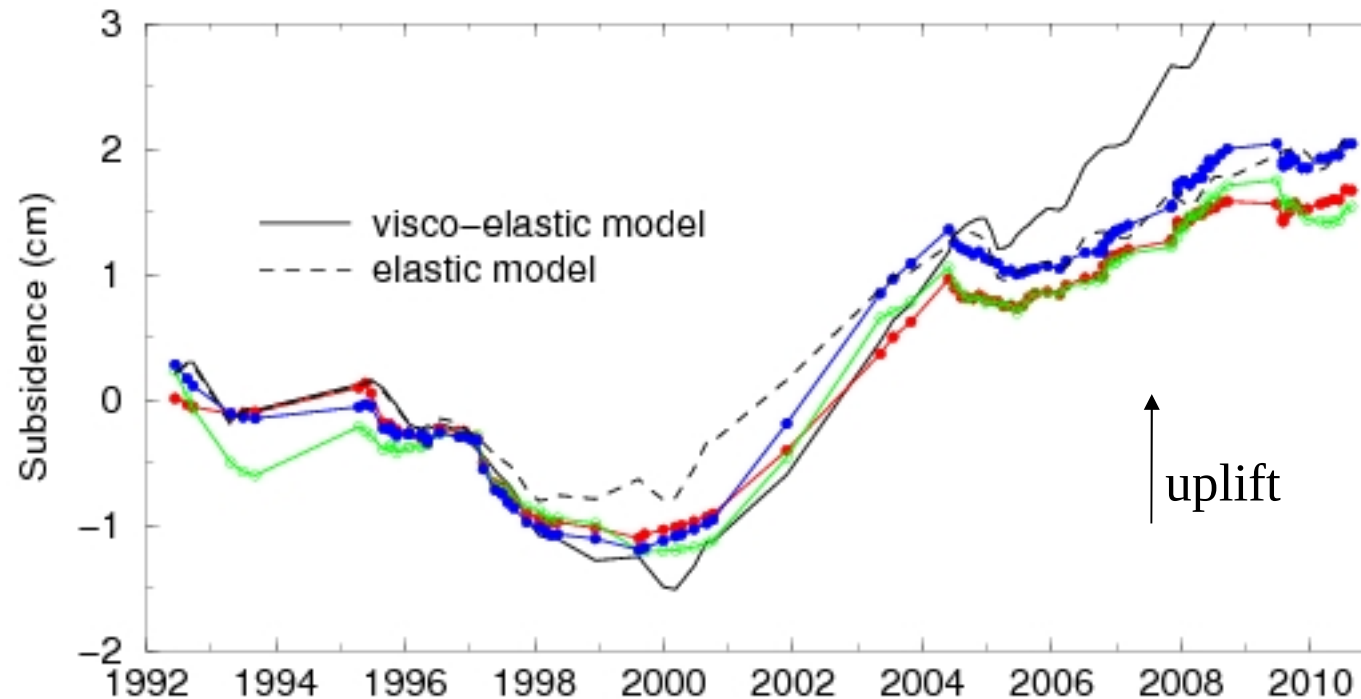
Very good correlation between load and ground motion : elastic ?

Modeling Forward predictions :

Layered Maxwell compressible viscoelastic model

- * **Elastic model**, constrained from V_p and V_p/V_s
 - 32 km crust : $\lambda = 36.5$ GPa, $\mu = 35.5$ GPa
 - uniform uppermost mantle : $\lambda = 72.6$ GPa, $\mu = 64.1$ GPa
- * **Viscoelastic model**
 - same elastic structure
 - uppermost mantle viscosity of 10^{18} Pa.s, elastic thickness of 32 km
(Kaufmann and Amelung, 2000)

Comparison with elastic and visco-elastic models



1992-2002 : follows the visco-elastic model
2004-2010 : follows the elastic model
==> exclude the viscosity of 10^{18} Pa.s

Conclusion :

- ◆ Detect **transient sub-centimeter ground motions** associated with water level fluctuations
 - At a **small spatial scale** (10x20 km² or less), clear delayed poro-elastic response of sedimentary layers to water level fluctuations. WELL DEFINED !
 - At **large spatial scale** (~ 100 x 100 km²), clear ground motion response to lake load variations.
 - ▶ Results are sensitive to the **phase/elevation correction** (atmospheric moisture)
 - ▶ Large scale atmospheric patches decrease the time series accuracy
- ◆ We now clearly exclude the viscosity structure given by Kaufmann and Amelung, although it provides a good fit to the 1992-2001 data.
==> Characterize the shape (G(x,y)F(t)) of the “non-elastic” signal ?

Atmospheric delays (e.g., Hanssen, 2001):

$$\text{Delay (m)} = 10^{-6} \int \left(k_1 \frac{P}{T} + k_2 \frac{e}{T} + k_3 \frac{e}{T^2} + k_4 W_{cl} - k_5 \frac{n_e}{f^2} \right) dz$$

Dry delay
~ 2.3 m

Wet delay
~ 0.3 m

Liquid delay
~ 4 mm

Ionosphere,
dispersive, ?

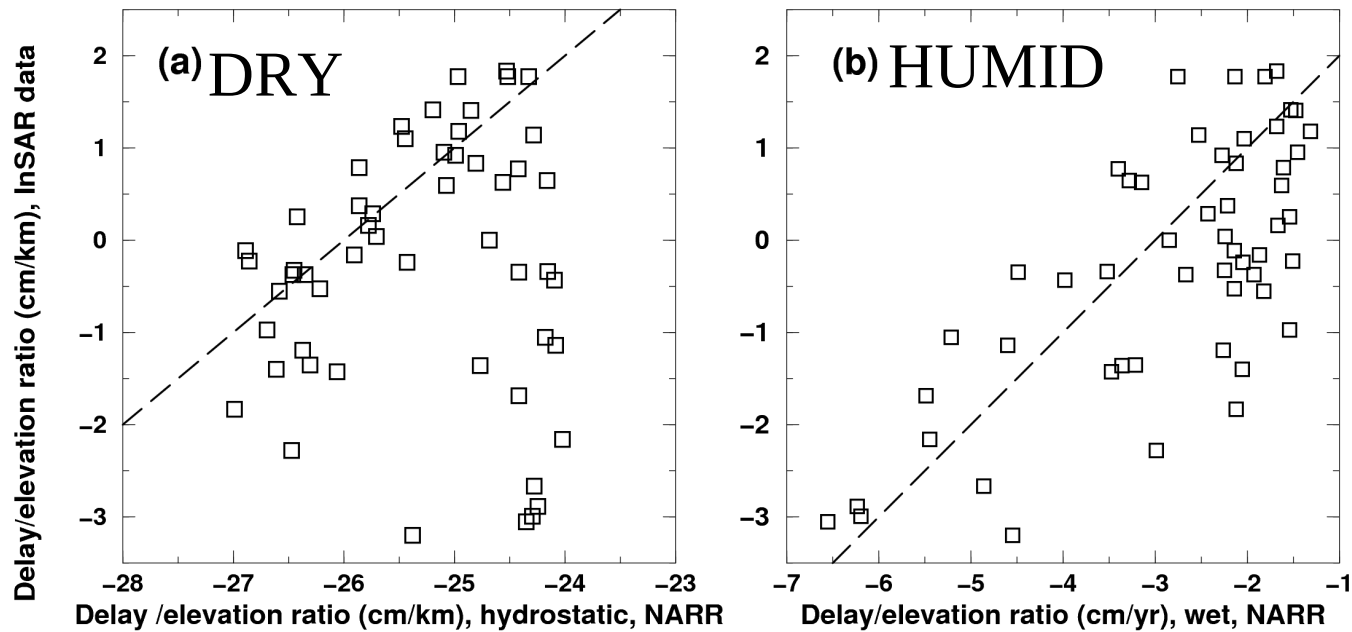
DInSAR :

- * blind to absolute delay
- * sees variations both in space and time (double differences)

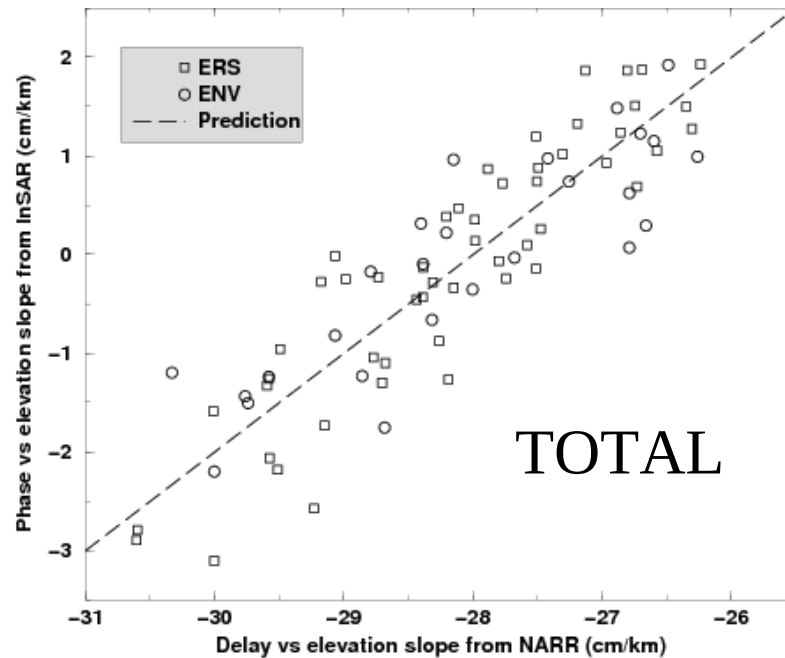
Two main effects :

- * Changes in atmospheric vertical stratification : leads a delay correlated with elevation
- * Atmospheric turbulence : random spatial patterns

Phase-elevation correlation : comparison with predictions derived from the North American Regional Analysis



COMPARISON
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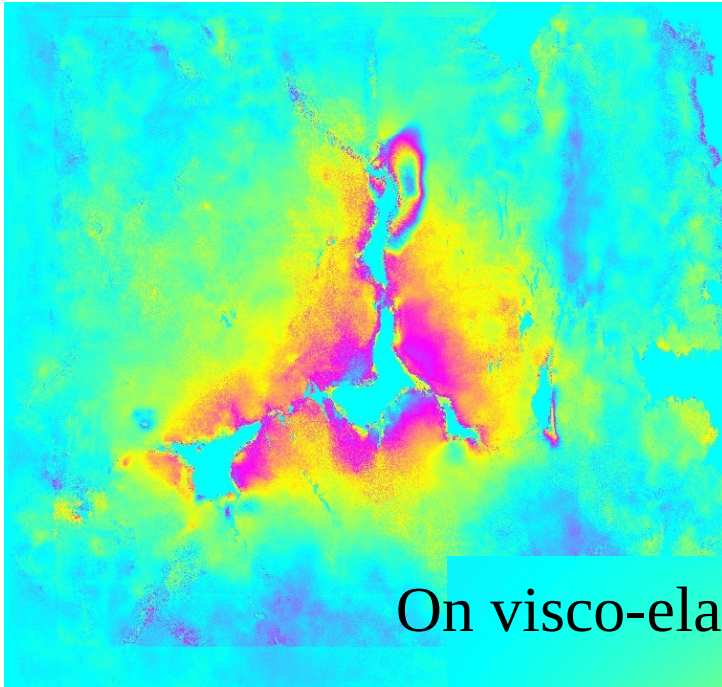


Doin et al.,
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Geophys., 2009

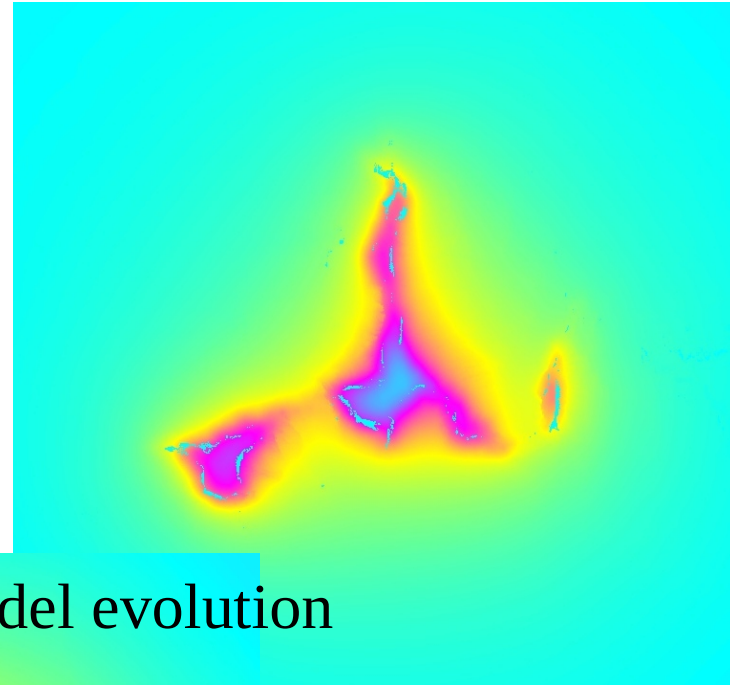
Spatial comparison using Principal Component Analysis

First eigen vector:

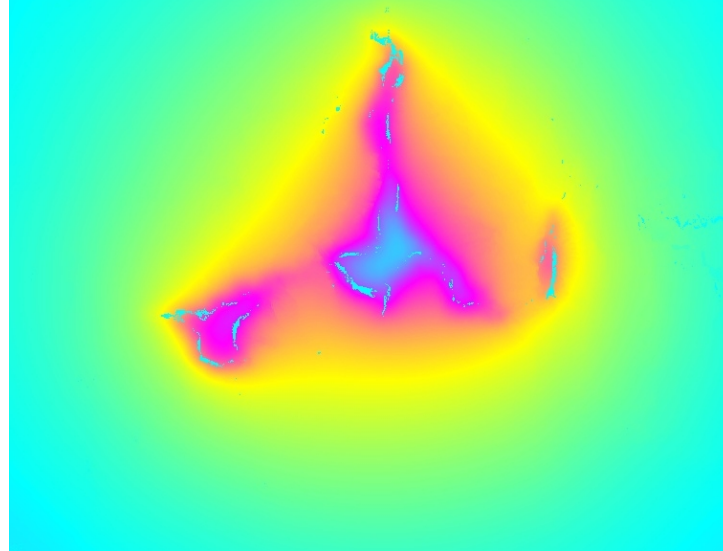
On raw phase delays

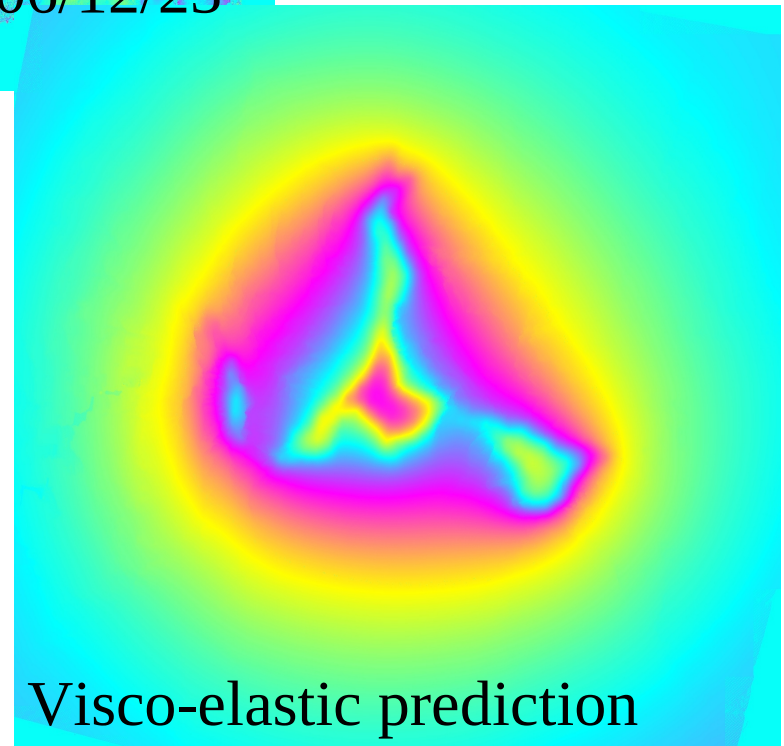
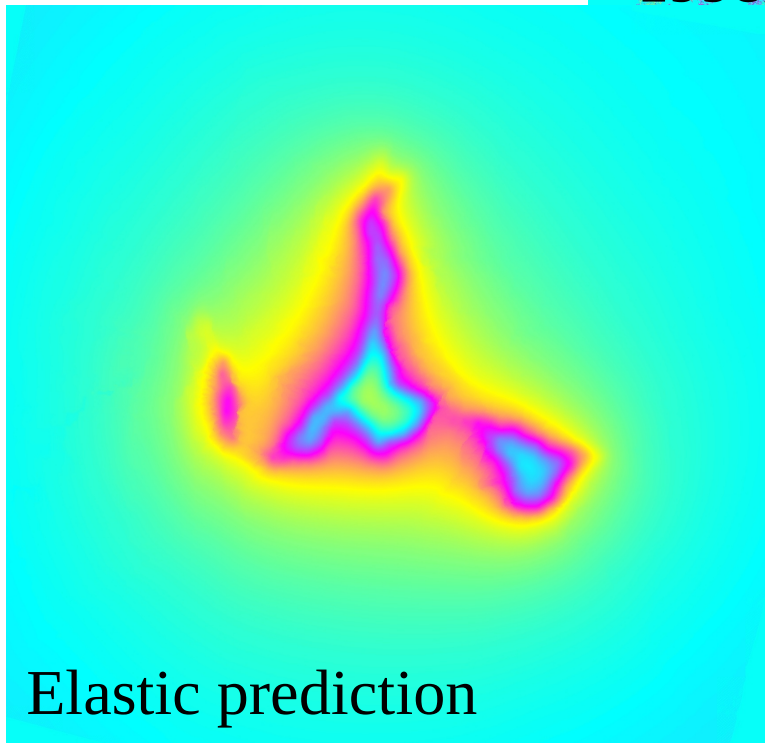
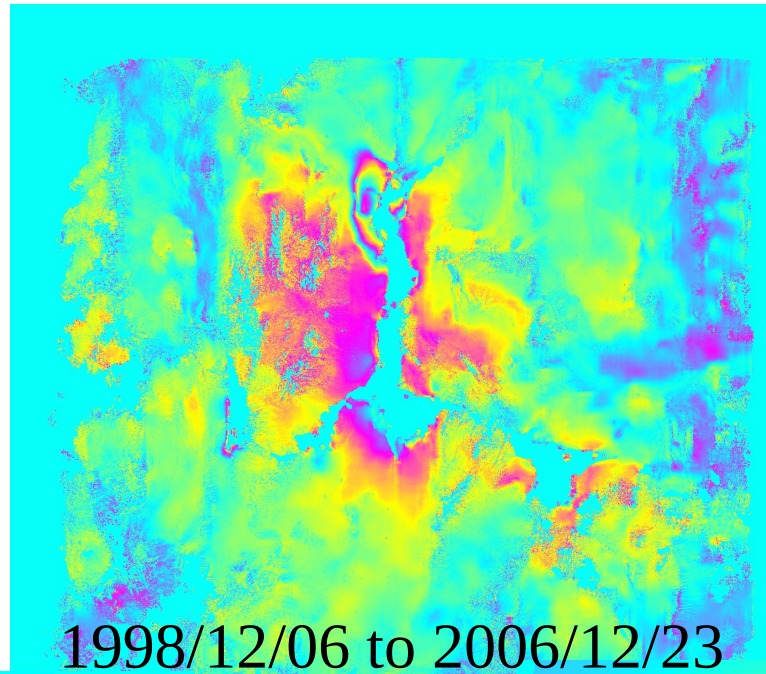


On elastic model evolution



On visco-elastic model evolution

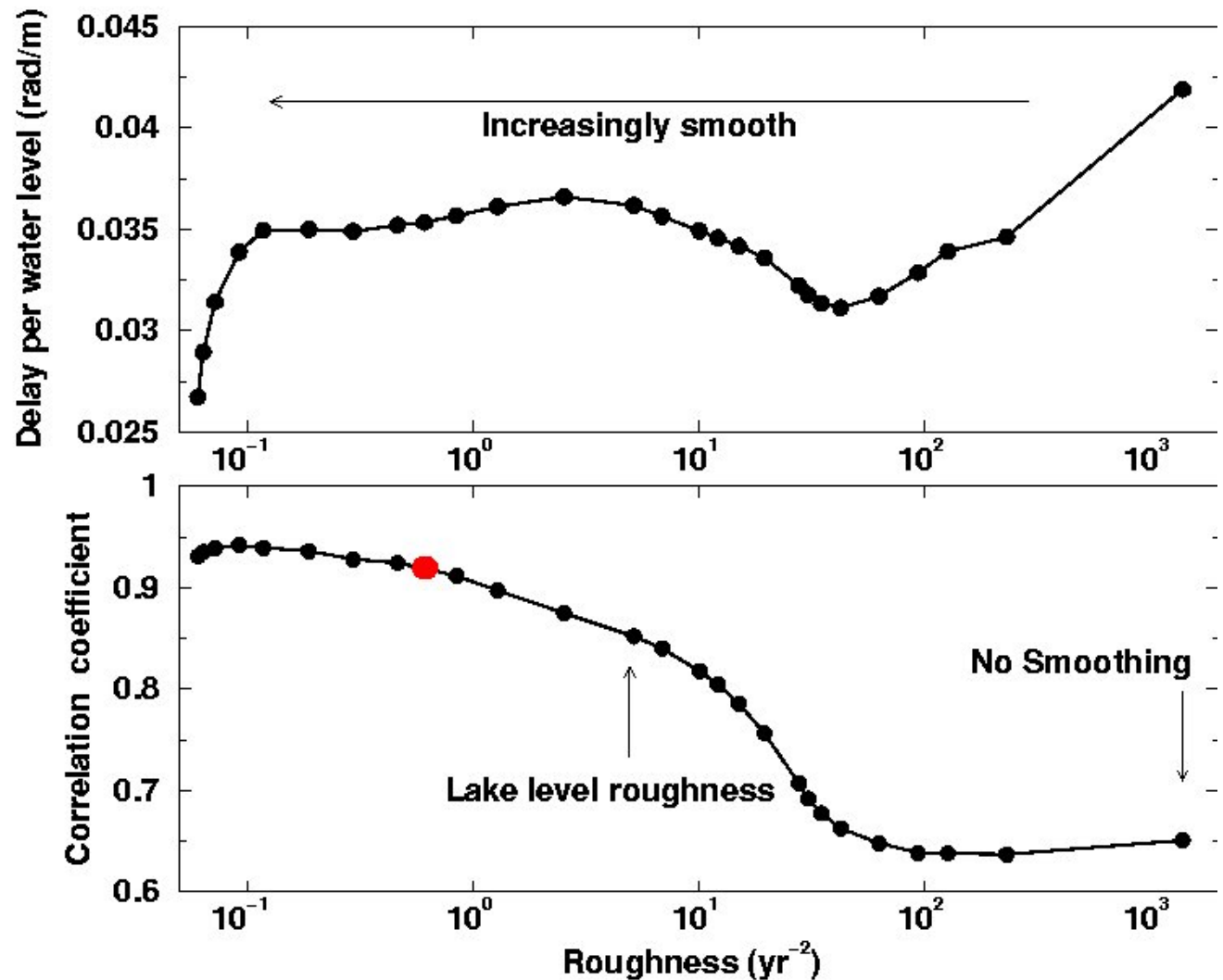




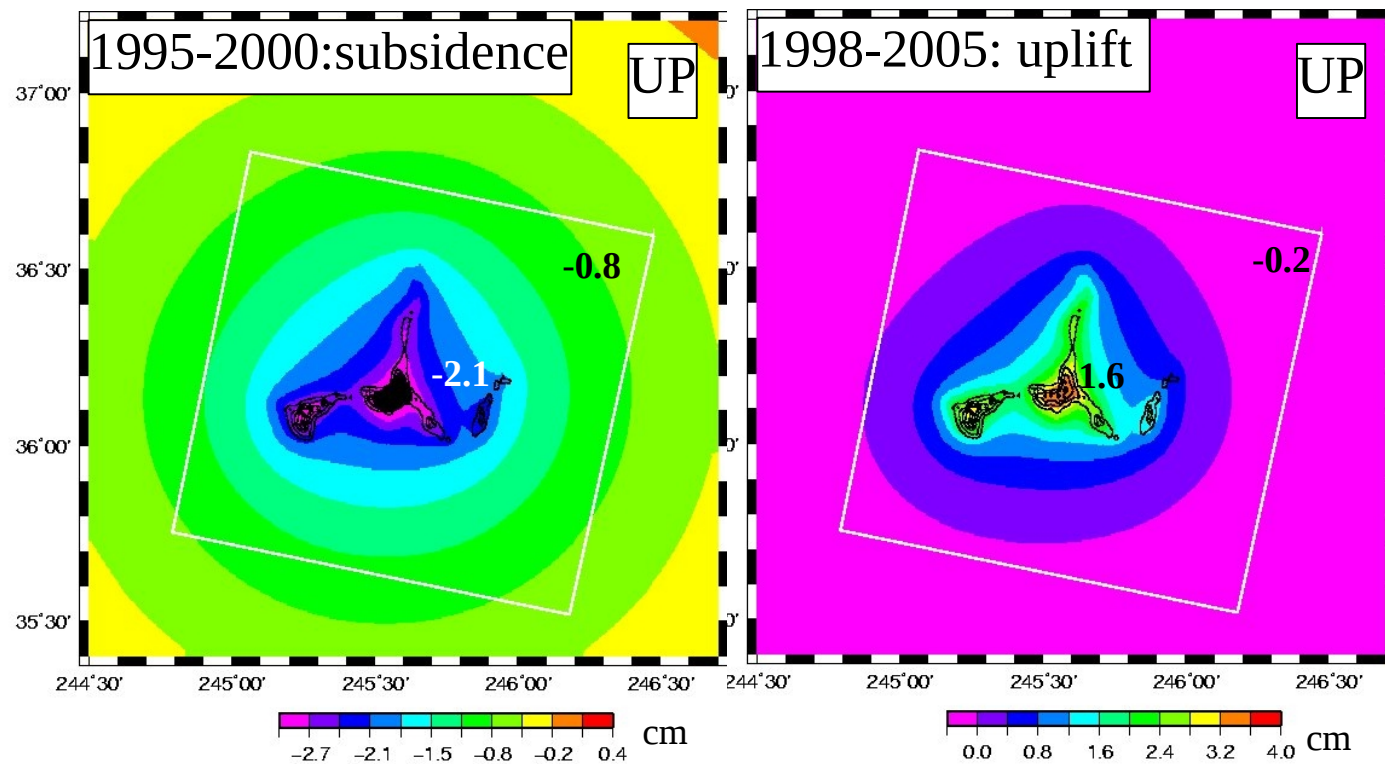
Inversion of interferograms into time series

- Effect of smoothing

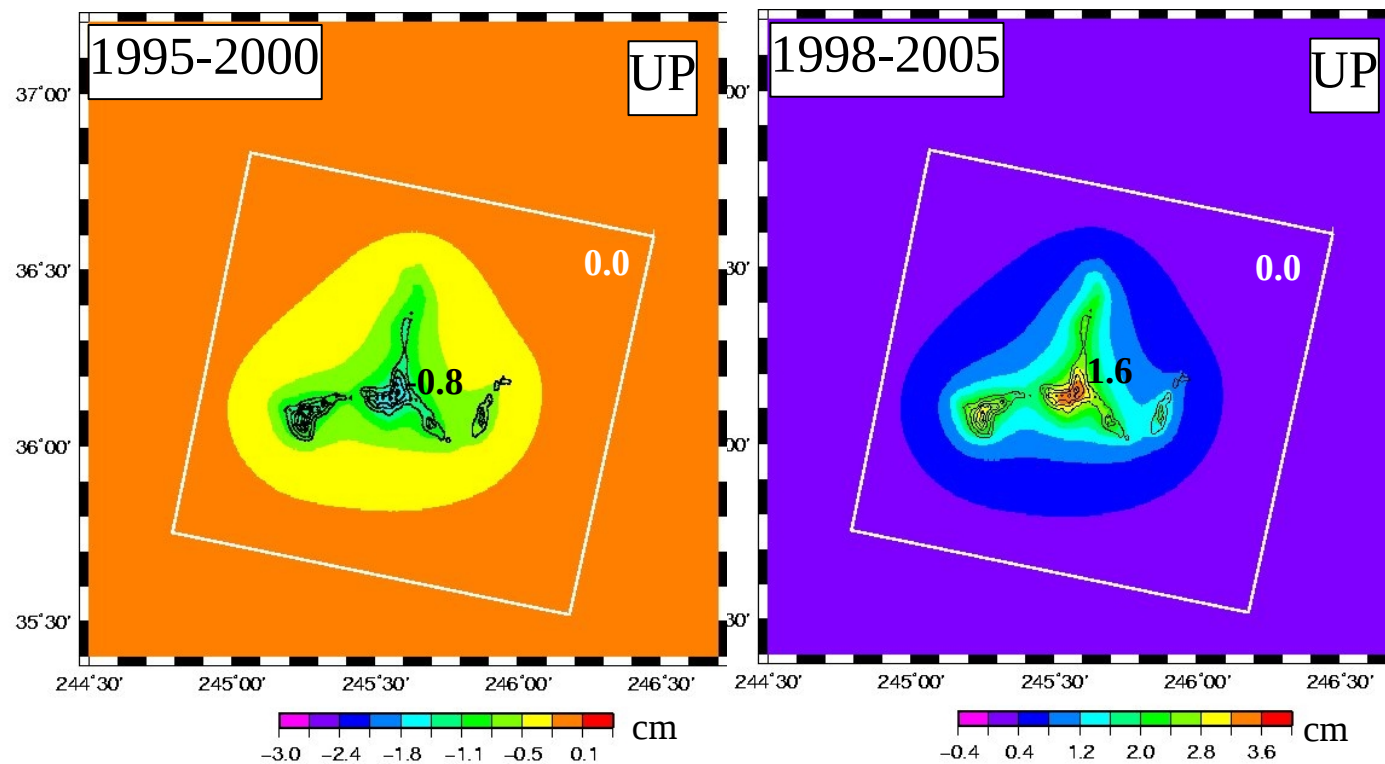
Correlation of
LOS displacement
with lake level
variations



Viscoelastic model

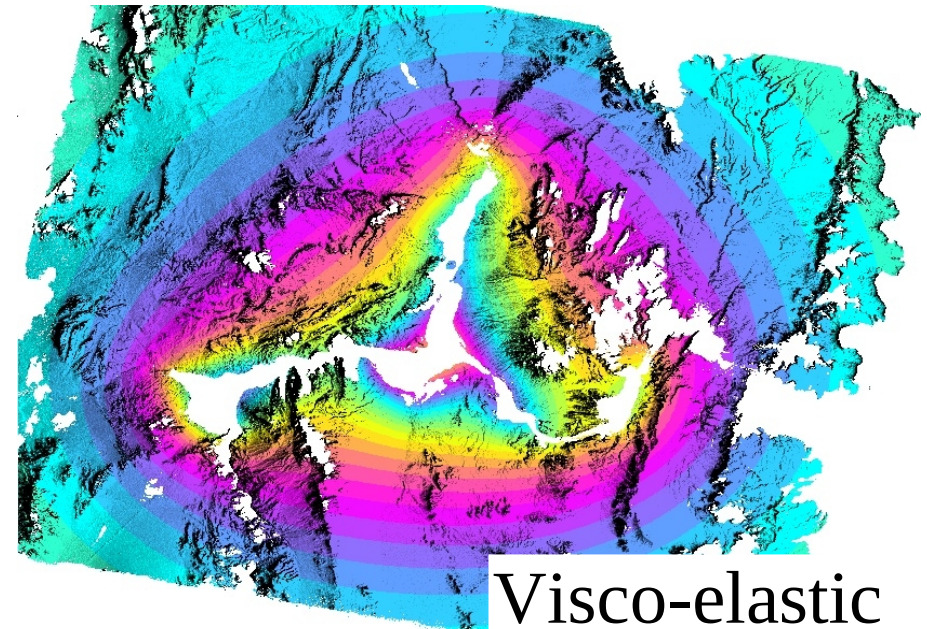
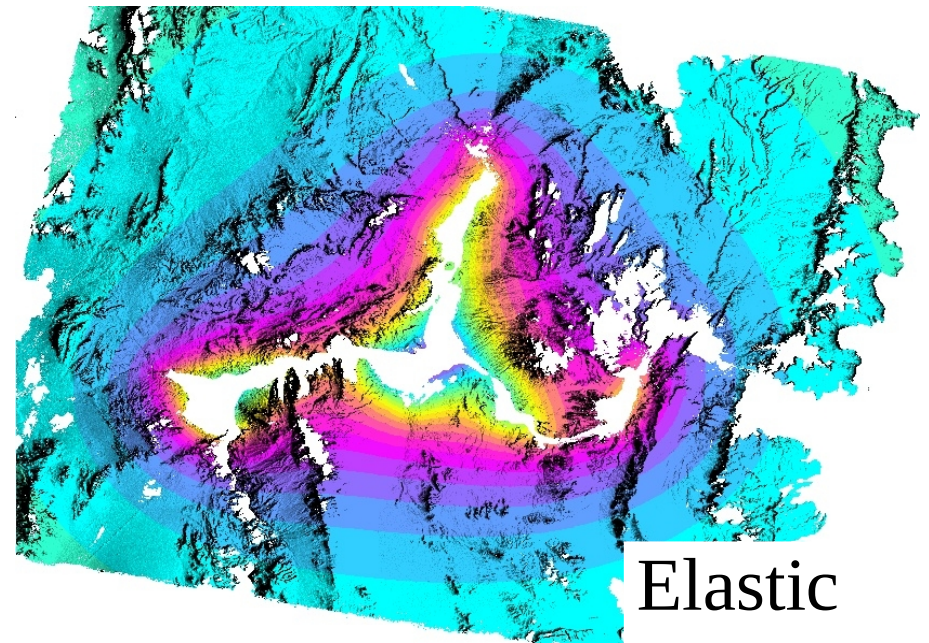
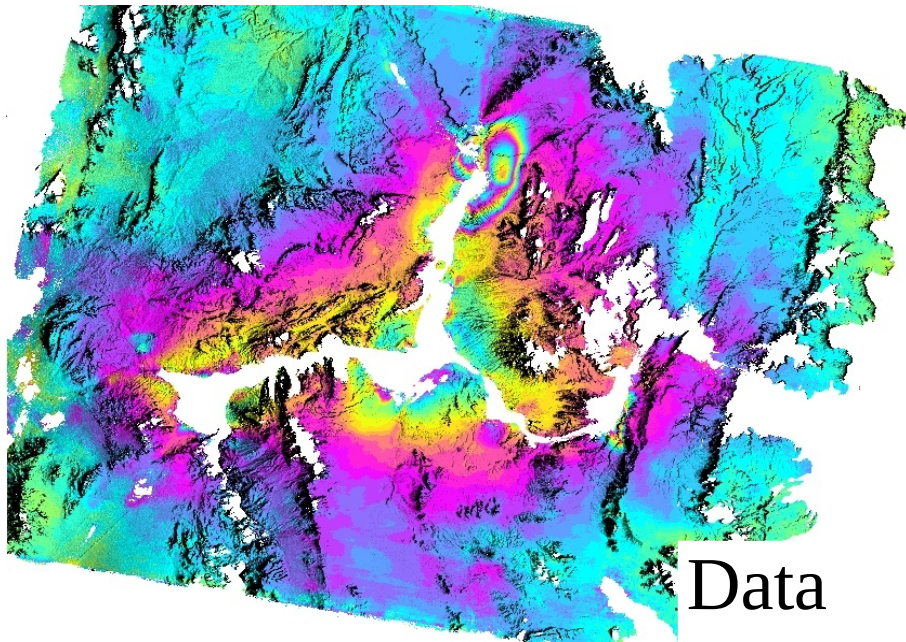


Elastic model



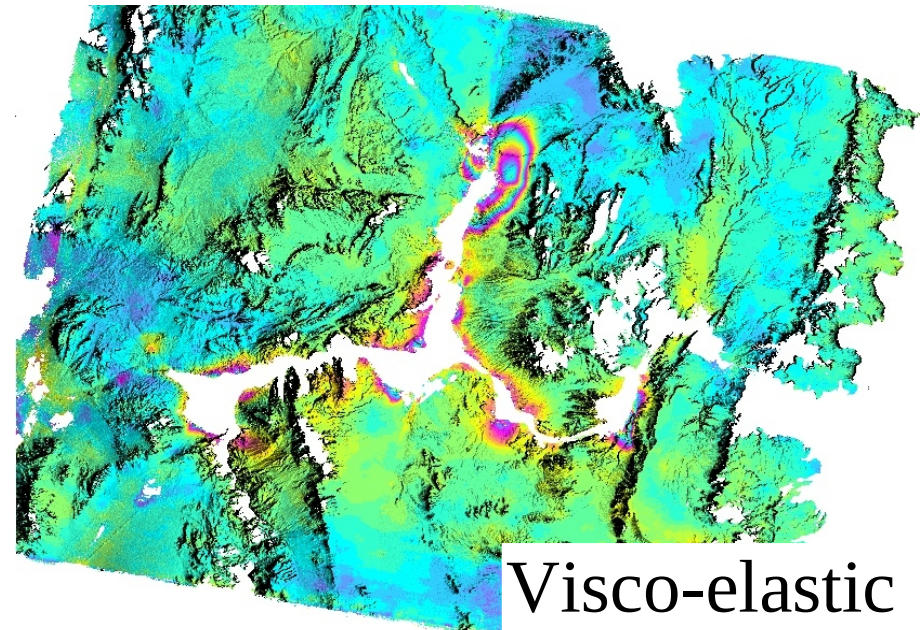
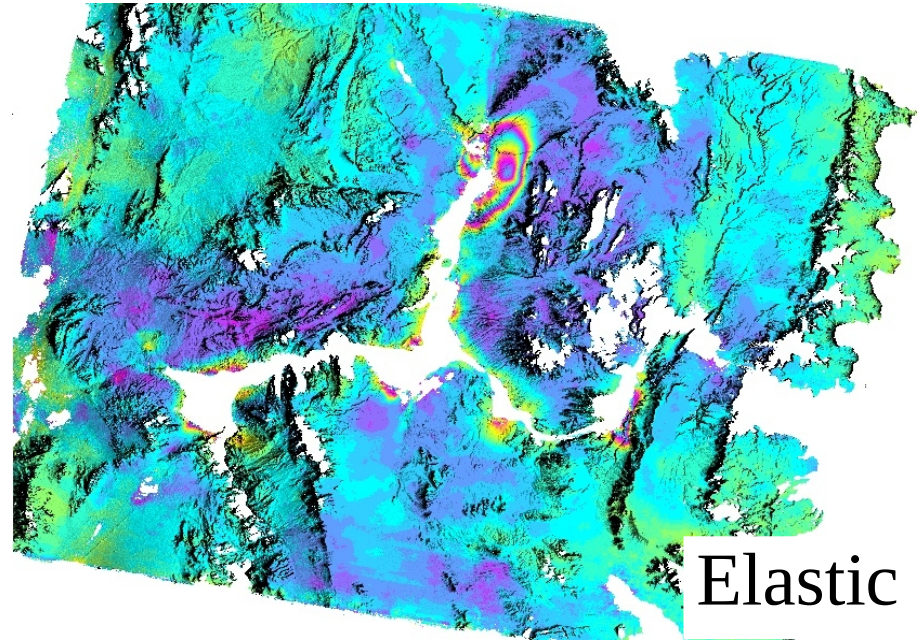
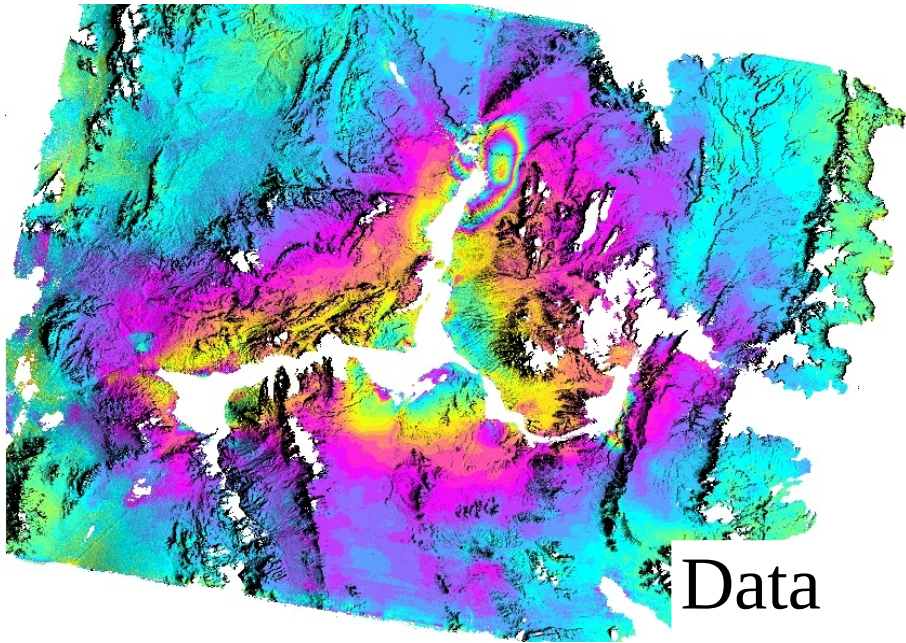
Comparison with forward elastic and visco-elastic models

Comparison between data stack
and model stacks



Comparison with forward elastic and visco-elastic models

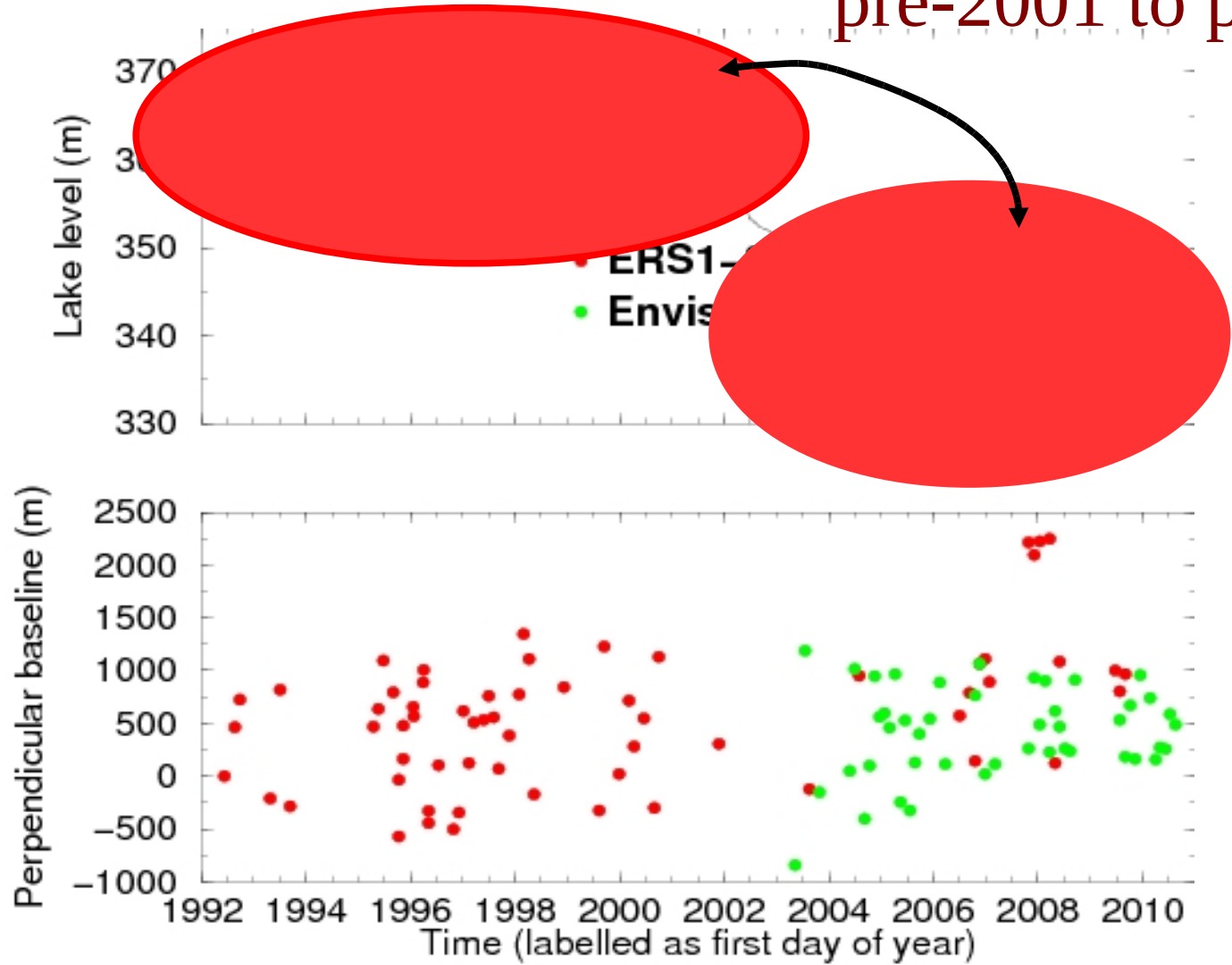
Residues



In between the two models ?
Larger viscosity than inverted
by K&A ?

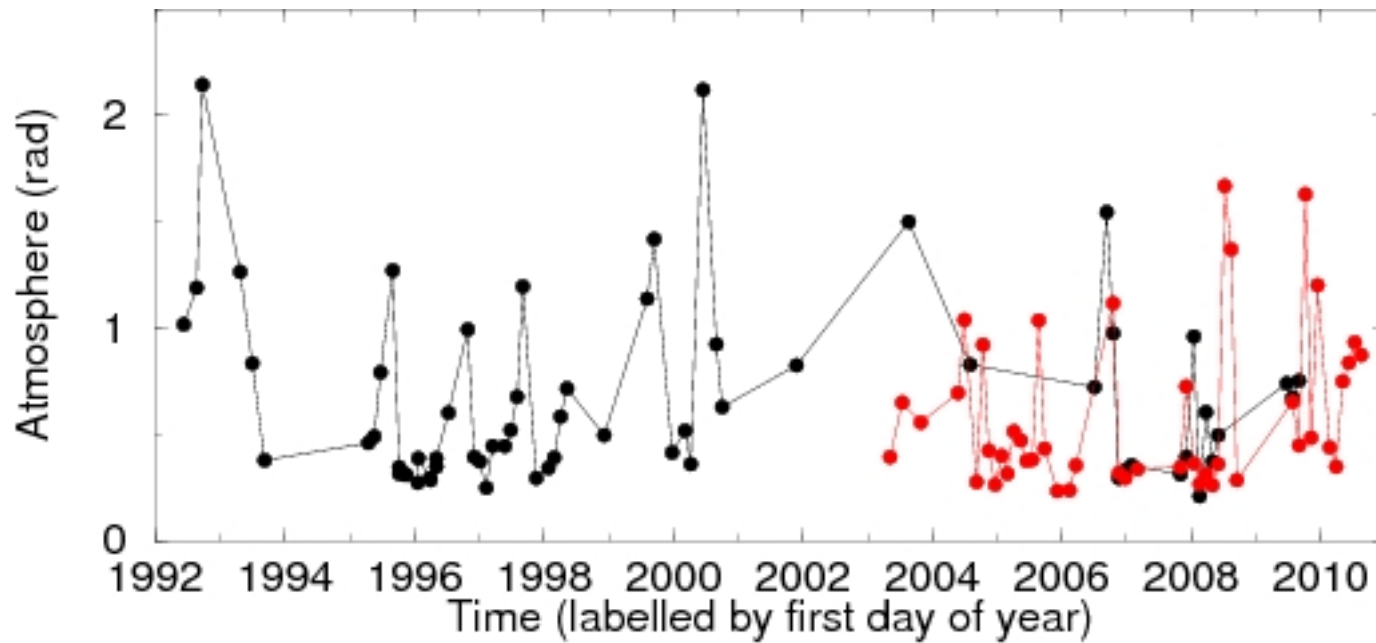
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pre-2001 to post-2003 links



ERS2 post-2000 images
squint angle variations :
small overlap in
doppler frequency in
azimuth

Amplitude of random patterns for each acquisition



Monsoon episodes
during summer with a strong
atmospheric turbulence

